

EC 313 Spring 2000 Problem Set 1

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Due Thursday 17 February 2000 at classtime

Produce a Mathematica notebook containing the answers to these questions, label it with your name, and email it (as an email attachment) to `baum@bc.edu` to submit your problem set. Where you are asked to say something about the results, put your comments in a cell of type “text” (that is, on the Format menu, select Style->Text). If you have any questions, please send me email.

1. a. Plot the $\sin(x)$ function over the range $\{-2\pi, 2\pi\}$.
b. The function `Nest[]` allows a function to be embedded within itself to an arbitrary depth. Plot the $\sin(x)$ function, nested 5 times, over the same interval.
c. Plot the $\sin(x)$ function, nested 100 times and 1000 times, over the same interval. What is happening to the function in terms of both shape and amplitude?
2. a. Define a function `f[x_]`, equal to $1/(1+x)$. The function `NestList[]` allows a function to be embedded within itself to an arbitrary depth, but returns a list of the successive evaluations. Apply `NestList[]` to your function `f[]` 6 times, using `x` as the expression to which the function should be applied.
b. Apply `NestList` to your function 20 times, using the number 1 as the starting expression. What pattern is evident in the numerators and denominators of the resulting fractions?
c. Apply `NestList` to your function 50 times, using the number 1 as the starting expression, and get the numerical evaluation of the result (using the `N[]` function). Does the sequence converge? How do these results relate to the so-called “golden ratio”? (hint: ask Mathematica about `GoldenRatio`).
3. a. Use the `Table[]` function to produce a table of x raised to the power i for $i = 0$ through 9.
b. Use `Table[]` and `TableForm[]` to produce a nicely formatted table of the product of $(x-j)$ for $i = 0$ through 5 and $j = 0$ through i .
c. A Vandermonde matrix $V(i,j)$ has elements defined as $x(i)^j$. Display a 5 by 5 Vandermonde matrix for `x`, with $i = 1$ through 5 and $j = 0$ through 4.
d. Calculate the symbolic determinant of this matrix (using `Det[]`) and use `Factor[]` to make it friendlier. Is there a discernable pattern?