Are New Keynesian Phillips Curves Identified?*

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Abstract

In this paper we use optimal-instrument and new finite-sample methods to test the empirical relevance of the New Keynesian Phillips curve (NKPC) equation. Unlike generalized method of moments-based methods, these generalized Anderson-Rubin tests are immune to the presence of weak instruments, and allow, by construction, to assess the identification status of a model. Our results are illustrated using the Gali-Gertler (1999) NKPC specifications and data, as well as a survey-based inflation expectation series from the Philadelphia Fed.

Our test rejects the reported Gali-Gertler estimates, conditional on their choice of instruments. Nevertheless, and in contrast to Ma (2002), we do obtain relatively informative confidence sets. This provides support for NKPC equations and illustrates the usefulness of using exact procedures and optimal instruments in IV-based estimations. In particular, our results reveal that firms fix prices in a predominantly backward-looking manner, but that they adjust prices every quarter or so. Furthermore, the outcomes indicate that it is difficult to pin-point the extent of the importance of marginal costs for the inflation process.

Keywords: NKPC, Anderson-Rubin Test, Optimal Instruments.

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1. Introduction

The New Keynesian Phillips curve (NKPC) equation resulted from the efforts of recent years to model the short-run dynamics of inflation starting from optimization principles. In its benchmark form, this equation stipulates that inflation a time t is a function of expected future inflation and current marginal costs. With its clearly-elucidated theoretical foundations, the NKPC possesses a straightforward structural interpretation and therefore presents a strong theoretical advantage to the traditional reduced-from Phillips curve (which is justified only statistically).

However, confronting the NKPC with the data has raised several issues[1]. In particular, modeling the marginal cost variable is a fundamental problem. Whereas, under some conditions, the output gap series is a natural proxy for this variable, studies using gap measures revealed empirical puzzles; in particular: (i) the coefficient on the output gap was estimated to be negative when theoretically it should be positive, and (ii) adding lagged inflation to the above model in an ad-hoc manner seemed to correct the estimated sign problem; suggesting that, unlike what the theory predicts, past inflation matters[2].

These results spurred further research on both the theoretical and empirical levels. For instance, Gali-Gertler(1999) modified the standard NKPC theoretical formulation by allowing a proportion of firms to use a rule of thumb when setting prices for their goods (rather than allowing all firms to set prices in a rational manner). The latter modification provides a theoretical justification for the presence of an inflation lag in the first-order-condition. Models which incorporate the above features are referred to as *hybrid* NKPC models.

On empirical grounds, efforts focused on proposing improved proxies for the marginal cost variable. For example, Gali-Gertler(1999) suggested using measures of marginal cost derived from a production function instead of relying on possibly-badly-measured output gaps. Generalized Method of Moments (GMM) estimation of the hybrid NKPC having these new marginal cost measures yielded the correct sign on that variable and the model was not rejected according to Hansen's J-test. Moreover, the choice for the marginal cost proxy seemed to affect the estimated weight of the backward- and forward-looking terms in the equation[3].

While the above outcomes appear encouraging, it is important to note that

[1] See, for example, Gali-Gertler(1999), Gali-Gertler-Lopez-Salido(2001), and the references cited therein.

[2] See, for example, Fuhrer-Moore(1995), Roberts(1997) and Fuhrer(1997).

[3] For example, see Gali-Gertler-Lopez-Salido(2001) and Gagnon-Khan(2001).

the recent literature on instrumental variable (IV) based inference casts serious doubts on the reliability of standard inference procedures[4]. These studies demonstrate that standard asymptotic procedures (i.e. procedures which *impose identification away* without correcting for local-almost-identification) are fundamentally flawed and lead to serious overrejections; these problems are not small-sample related and occur with fairly large sample sizes, since they are caused by asymptotics failures. In particular Dufour(1997) shows that usual t-type tests, based on common IV estimators, have significance levels that may deviate arbitrarily from their nominal levels since it is not possible to bound their null distributions.

To circumvent weak-instruments related difficulties, the above-cited work on IV-based inference has focused on three main directions: (i) refinements in asymptotic analysis which include the local-to-zero or local-to-unity frameworks (e.g. Staiger-Stock(1997), Wang-Zivot(1998), and Stock-Wright(2000)), (ii) proposing asymptotic approximations which hold whether instruments are weak or not (e.g. Kleibergen(2002), Moreira(2003)), and (iii) developing new finite-sample-justified procedures based on proper pivots – that is, finding statistics whose null distributions are either nuisance-parameter-free or are bounded by nuisance-parameter-free distributions (e.g. Dufour(1997), Dufour-Jasiak(2001), Dufour-Khalaf(2002), and Dufour-Taamouti(2003b,c)).

Clearly, the question of whether the NKPC is supported by the data begs re-examination using some of these more reliable econometric methods. Such an excercise was undertaken recently by Ma (2002), who used the asymptotic test statistics proposed in Stock and Wright (2000) to evaluate the empirical relevance of the Gali-Gertler NKPC specifications. He concluded that weak identification was a major concern in these models, and that there was an unreasonably large set of parameter values that were compatible with these models.

In this paper, we focus on the new finite-sample methods, with and without optimal instruments, to test the empirical relevance of the NKPC. The latter methods allow, by construction, to assess the identification status of a model. Another major advantage they have is that they are valid in samples typical of macroeconomic data – i.e. fairly small. Furthermore, they can provide fairly detailed information regarding the nature of potential under-identification, suggesting useful theory modifications. This is an advantage compared to the Stock and Wright asymptotic methods because the latter do not provide such information directly. As for the optimal instruments, these are derived using the methods proposed in Dufour (2003), Dufour and Taamouti (2003b,c), and Du-

[4]see for example Dufour(2003), Stock-Wright-Yogo(2002), and the references cited therein.

four and Khalaf (2003). The former two studies show when the AR test with optimal instruments is equivalent to the Wang-Zivot (1998) LM test, and the circumstances under which the test is exact. The latter shows the equivalence of the optimal-instrument AR test to Kleibergen's K-test.

Specifically, we apply the econometric methods presented in Dufour and Jasiak (2001), which are generalizations of the Anderson-Rubin statistics, with and without optimal instruments. Like Ma (2002), our results are illustrated using the Gali-Gertler NKPC specifications and data. In the next section we reproduce the NKPC models that were developed by Gali and Gertler (1999), as well as their and Ma's results. In Section 3, we present the generalized Anderson-Rubin (hereafter AR) test. Section 4 documents and discusses the results of the AR test applications with selected instruments to the above NKPC specifications. A subsection presents the methods of obtaining optimal instruments and their applications to the hybrid NKPC. The last section concludes.

The Gali-Gertler NKPC models

In Gali-Gertler's benckmark specification all price-setting firms are forward-looking in a monopolistically-competitive environment. Thus, inflation, π_t, is a function of next period's expected inflation, $E_t\pi_{t+1}$, and real marginal costs, s_t (expressed in percent deviation with respect to its steady-state value). Specifically, the model is given by:

$$\pi_t = \lambda_1 s_t + \beta E_t \pi_{t+1}, \tag{1}$$

with

$$\lambda_1 = \frac{(1-\theta)(1-\beta\theta)}{\theta}, \tag{2}$$

and where θ is the proportion of firms that do not adjust their prices in period t, β is the subjective discount rate, and $E_t\pi_{t+1}$ is the value of inflation for next period that is expected at time t.

In contrast, Gali-Gertler's hybrid specification assumes that some of the firms use a rule-of-thumb when setting their prices. The proportion of such firms (referred to as the backward-looking price setters) is given by ω. In this case, the model is written as:

$$\pi_t = \lambda_2 s_t + \gamma_f E_t \pi_{t+1} + \gamma_b \pi_{t-1}, \tag{3}$$

with

$$\begin{aligned} \lambda_2 &= \frac{(1-\omega)(1-\theta)(1-\beta\theta)}{\theta+\omega-\omega\theta+\omega\beta\theta} \\ \gamma_f &= \frac{\beta\theta}{\theta+\omega-\omega\theta+\omega\beta\theta} \\ \gamma_b &= \frac{\omega}{\theta+\omega-\omega\theta+\omega\beta\theta}, \end{aligned} \tag{4}$$

and where π_{t-1} is the inflation lag, γ_f is the forward-looking component of inflation, and γ_b is its backward-looking part.

The authors assume rational expectations and re-write the above NKPC models in terms of orthogonality conditions to be estimated by standard two-step GMM. Because of small-sample concerns, each re-written model is normalized in two ways: (i) so as to minimize non-linearities (denoted specification (1)), and (ii) setting the inflation coefficient equal to one (denoted specification (2)).

The data used is quarterly U.S. data, with π_t measured by the percentage change in the GDP deflator, and real marginal costs given by the logarithm of the labour income share[5]. The instruments used include four lags of inflation, labour share, commodity-price inflation, wage inflation, long-short interest rate spread, and output gap (measured by a detrended log GDP).

For their benchmark model, Gali-Gertler find values of (θ,β) equal to (0.83,0.93) and (0.88,0.94) for their specifications (1) and (2) respectively. Constraining β to 1 yields similar results, namely $\theta = 0.83$ in (1) and $\theta = 0.92$ in (2). The implied slope coefficients on the marginal cost variable for all these cases is positive and significant – based on the IV-based asymptotic standard errors, and the overidentifying restrictions are not rejected according to the J-test. For their hybrid model, the same normalizations and instrument set are used. In this case, the obtained values for ω, θ, and β are (0.27,0.81,0.89) and (0.49,0.83,0.91) for specifications (1) and (2) respectively. In the restricted cases, these are (0.24, 0.80,1.00) and (0.52,0.84,1.00) respectively. Again, the implied slopes are all positive and found to be significant.

Based on these, and some additional GMM estimations carried out for robustness purposes, the authors conclude that there is good empirical support for the NKPC, and furthermore, that the forward-looking component of inflation is more important than the backward-looking part.

Despite these significant outcomes, it is important to be wary of GMM-based outcomes, as the severity of weak-instruments effects is now well-understood in

[5]They also report results for the case where inflation is measured by the non-farm deflator. These yield similar outcomes to those based on the GDP total deflator measure.

econometrics[6]. Given these concerns, Ma (2002) uses the test statistics developed by Stock and Wright (2000) to re-evaluate the empirical relevance of these NKPC specifications. These asymptotic methods account for the presence of weak instruments and provide corrected confidence intervals for the GMM-estimated parameters.

Ma first notes that the benchmark model presents a theoretical identification problem; namely that there is an observational equivalence between the sets (β, θ) and (β, $1/\beta\theta$). Thus, there is more than one parameter combination that satisfies the GMM minimization criterion. In other words, the objective function being solved by GMM (and which is concentrated with respect to θ) is non-quadratic. Therefore, conventional tests, such as those applied in Gali-Gertler, do not provide accurate information on the precision of GMM estimates.

Turning to the estimates from the hybrid model, Ma calculates the corrected confidence set according to the method proposed in Stock and Wright (2000). He finds that the 90% S-set is particularly large, including all parameter values between [0,3] for two of the parameters, and [0,8] for the third. That is, all parameter combinations derived from these value ranges are compatible with the model. This is a clear indication of weak identification in this model.

Thus, the validity of the Gali-Gertler GMM-based estimates is in question. But, the Stock and Wright intervals provide little concrete direction in which theoretical research should be oriented. On the other hand, the recently-advanced finite-sample methods that also deal with the possible presence of weak instruments may be able to point to such directions. In the next section, we present a test strategy belonging in the latter finite-sample category. It is one proposed in Dufour and Jasiak (2001) and is a generalization of the Anderson-Rubin (1949) technique.

The AR test

The Anderson-Rubin test has recently received renewed interest[7]. In its generalized form – developed by Dufour and Jasiak (2001) – it is applicable to univariate models using limited information, and where one or more of the right-hand-side variables are possibly endogenous.

[6]Examples include Dufour(1997), Staiger-Stock(1997), Wang-Zivot(1998), Stock-Wright(2000), Dufour-Jasiak(2001), Stock-Wright-Yogo(2002), Kleibergen-Zivot(2003), Khalaf-Kichian(2002), Dufour-Khalaf(2003), Dufour-Taamouti(2003b,c) and Dufour(2003).

[7]See, for example, Dufour(1997), Staiger-Stock(1997), Dufour-Jasiak(2001), Dufour-Khalaf(2003), and Dufour-Taamouti(2003b,c).

More formally, consider a limited information simultaneous equations system

$$y = Y\delta + X_1\kappa + u, \tag{5}$$

where y is an $n \times 1$ dependent variable, Y is an $n \times m$ matrix of endogenous variables, X_1 is an $n \times k_1$ matrix of exogenous variables, and u is an error term which satisfies standard regularity conditions typical to IV regressions; see Dufour-Jasiak(2001).

In this context, consider hypotheses of the form

$$H_0 : \delta = \delta^0. \tag{6}$$

Define $\tilde{y} = y - Y\delta^0$ so that under the null hypothesis, (6) implies

$$\tilde{y} = X_1\kappa + u. \tag{7}$$

In view of this, the AR test is based on assessing the exclusion of X_2 (of size $n \times k_2$) in the regression of $\tilde{y}$ on X_1 and X_2, which can be conducted using the standard F-test or its chi-square asymptotic variant; see Dufour-Jasiak(2001). Let $X = (X_1, X_2)$, and define

$$\begin{aligned} M &= I - X(X'X)^{-1}X' \\ M_1 &= I - X_1(X_1'X_1)^{-1}X_1' \end{aligned}$$

then the statistic takes the form

$$AR = \frac{\left[\left(y - Y\delta^0\right)' M_1 \left(y - Y\delta^0\right) - \left(y - Y\delta^0\right)' M \left(y - Y\delta^0\right)\right] / k_2}{\left(y - Y\delta^0\right)' M \left(y - Y\delta^0\right) / \left(n - k_1 - k_2\right)}. \tag{8}$$

Under the null hypothesis and imposing strong exogeneity and i.i.d. normal errors, $AR \sim F(k_2, n - k_1 - k_2)$; the normality and i.i.d. hypotheses can be relaxed so under standard regularity conditions and weakly exogenous regressors, $(k_2 \times AR) \overset{asy}{\sim} \chi^2(k_2)$.

The test can be readily extended to accommodate additional constraints on the exogenous variables coefficients; see Maddala(1974), Dufour-Jasiak(2001), Dufour-Taamouti(2003b,c) and Dufour(2003). Specifically, consider a hypothesis of the form:

$$H_0 : \delta = \delta^0, \quad \kappa_1 = \kappa_1^0, \tag{9}$$

where κ_1 is a subset of κ, i.e. $\kappa = (\kappa_1', \kappa_2')'$. Partition the matrix X_1 (into X_{11} and X_{12} sub-matrices) accordingly and let

$$\breve{y} = y - Y\delta^0 - X_{11}\kappa_1, \tag{10}$$

so the restricted model becomes

$$\breve{y} = X_{12}\kappa_{12} + u, \tag{11}$$

and the test may be carried out as above.

While the test in its original form was derived for the case where the first stage regression is linear, Dufour-Taamouti(2003b,c) have shown that it is in fact robust to: (i) the specification of the model for Y, and (ii) excluded instruments; in other words, the test is valid whether the first stage regression is linear or not, or whether the matrix X_2 includes all available instruments or not. As argued in Dufour(2003), since one is never sure that all instruments have been accounted for, the latter property is quite important. Most importantly, this test (and several variants discussed in Dufour(2003)) is the only truly pivotal statistic whose properties in finite samples are robust to the quality of instruments.

Applications of the AR test

The econometric models that we use for the AR applications are the Gali-Gertler benchmark and hybrid models in equations (1) and (3) respectively, with $E_t\pi_{t+1}$ given by a survey measure of inflation expectations, $\tilde{\pi}_{t+1}$. The Federal Reserve Bank at Philadelphia publishes quarterly mean forecasts of the next quarter US GDP implicit price deflator, which we first difference to obtain our inflation expectations series[8]. A measurement error term u_t is added to the equation to reflect the fact that the expectations variable is a proxy. Thus, our econometric equivalents of the Gali-Gertler models are:

$$\pi_t = \lambda_1 s_t + \beta\tilde{\pi}_{t+1} + u_t, \tag{12}$$

and

$$\pi_t = \lambda_2 s_t + \gamma_f\tilde{\pi}_{t+1} + \gamma_b\pi_{t-1} + u_t, \tag{13}$$

where λ_1, λ_2, γ_f, and γ_b are defined as previously (see equations (2) and (4)).

In this framework, and for both the benchmark and hybrid models, $y = \pi_t$, $Y = (s_t, \tilde{\pi}_{t+1})'$, and X_2 is the 24-variable set of instruments used by Gali-Gertler. In addition, X_1 is zero in the benchmark case, and equal to π_{t-1} in the hybrid case.

We test the Gali and Gertler (1999) estimates for the benchmark and hybrid models, and for both specifications, using their instrument set each time[9]. An

[8]Source: http://www.phil.frb.org/econ/spf/index.html.

[9]Due to the presence of the expectations variable our sample starts in 70:1.

illustration is as follows: say we want to test their benchmark model specification (1) estimates. We impose $\theta = 0.83, \beta = 0.93$, and calculate the corresponding slope value, which is $\lambda_0 = 0.05$. The null hypothesis for the AR test is then given by: $H_0 : \lambda_0 = 0.05$ and $\beta_0 = 0.93$. Constructing $\tilde{y}$, we regress it on all the Gali-Gertler instruments. We also obtain the M and M_1 matrices as in equations (8). With these, we compute the value of the AR statistic according to equation (8). We have $n = 112$ observations and $k_2 = 24$ instruments. The statistic is therefore compared to the F(24,88) distribution, and in the case where the normality and i.i.d. hypotheses are relaxed, 24×AR is compared to a $\chi^2(24)$.

The results are reported in Table 1. From there, we can see that all of the Gali-Gertler GMM estimates are decisively rejected at the 5% level. In other words, given the instrument set that was used by Gali and Gertler, both their benchmark and hybrid models are strongly rejected by the data, whether specification (1) or (2) estimates are used, and whether the β parameter is restricted to equal 1.

Next we ask whether, for the same instrument set, there are any parameter combinations for which the models are not rejected. Thus, we conduct such a grid search for each of the benchmark and hybrid models, allowing the range (0,1) as the admissible space for ω, θ, and β, and varying these values with increments of 0.1. We find that all parameter combinations reject the model at the 5% level, whether it is the benchmark or the hybrid equation that's being tested.

This conclusion is in striking contrast with the findings of Ma (2002), although both our results highlight the weak-instrument problem emphatically. That is, while the Stock-Wright asymptotic test finds that all parameter combinations do not reject the model, we find that all of them actually reject it. Therefore, it appears that the AR-test has more power compared to the Stock-Wright methodology[10].

Selected Instrument Sets

It is evident that whether a model is rejected or not depends on the instruments that are used to specify it. An easy way to understand the relevance of various instrument sets is to specify the model with each and then test it. We consider seven different instrument sets, each comprised of 4 lags of a variable amongst

[10] Although, we note that there is a slight difference in our two instrument sets: Ma's set includes a constant and has no 4th lag for each of the three variables in levels.

the following: GDP deflator inflation, wage inflation, commodity price inflation, labor income share, long-short interest rate spread, quadratically-detrended output gap, and cubically-detrended output gap[11]. For each of these sets, we conduct grid searches for the benchmark and hybrid models again, always admitting a (0,1) range for each of ω, θ, and β, and still varying the parameter values by increments of 0.1.

The results are tabulated in Tables 2-3b, and 8a-10b. Table 2 shows, for the seven instrument sets, those combinations of β and θ values that do not reject the tested benchmark specification. The remaining Tables are results for the hybrid model. Tables 3a-3b show the outcomes for estimations over the full sample, while Tables 8a-8b, 9a-9b, and 10a-10b in the Appendix tabulate results for non-intersecting sub-samples (70:1-79:4, 80:1-89:4, 90:1-97:4). In each case, we report the results with four of the instrument sets[12].

Overall, results show that there are parameter combinations for which a given model is rejected, and others for which it is not. Second, some instrument sets appear to have more informational content than others (i.e. they yield a smaller set of parameter combinations that do not reject the model). These results are somewhat positive for macroeconomic theorists because they indicate that the NKPC models are not rejected outright. But while the scope of the identification issue is slightly less dramatic with our results than with those suggested by the Stock-Wright method, our various tables do indeed indicate the presence of pervasive identification problems. For instance, in the benchmark model, the instrument sets in columns 1-4 and in column 6 show that there are many parameter combinations for which the model is valid. Similarly, in the hybrid model case, there are numerous parameter combinations that do not reject the NKPC specification.

However, an important fact is that additional information can be gained from the examination of these tables regarding the direction in which theoretical research should be oriented. In particular, with the hybrid model case, some patterns emerge: (i) as the value of θ increases, the values for β decrease, and (ii) results are more restrictive when ω is not too high or too low. Based on

[11] For our output gap measure, and for all the tests we conduct, rather than detrending the log of GDP using the full sample, n, we proceed iteratively: to obtain the value of the gap at time t, we detrend GDP with data ending in t. We then extend the sample by one more observation and re-estimate the trend. This is then used to detrend GDP and yields a value for the gap at time $t+1$. And so on till the end of the sample. In this fashion, our gap measures at time t do not use information beyond that period and can therefore be used as valid instruments.

[12] This is to save space. The remaining tables are available upon request.

these, we can see that if one is willing to assume a range for the subjective discount rate that is economically meaningful (say, values ranging from 0.8 to 1), then the space of admissible parameter values is greatly reduced: thus θ is almost never above 0.4, and it is lower when ω is either high or low. That is, the ω parameter is less well-identified than θ, which implies that research needs to find better ways of characterizing the inertia in inflation dynamics.

The information in the above tables has been summarised in a number of graphs. For each model, we show the graphs for the parameter combinations that do not reject the model when the latter is specified using four different instrument sets. Figure 1 presents the graphs for the benchmark model for the instrument sets: lags 1 to 4 of inflation, lags 1 to 4 of wage inflation, lags 1 to 4 of the long-short spread, and lags 1 to 4 of labor income share. Figure 2 depicts graphs for the hybrid model with the same instrument sets. Column 1 shows the graphs for θ and β for all values of ω considered, while the subsequent columns show θ and β for $\omega = 0.2$, $\omega = 0.5$, and $\omega = 0.8$ respectively. Figures 8, 10 and 12 in the Appendix depict each similar graphs to Figure 2, but for the subsamples 1970:1-1979:4, 1980:1-1989:4, and 1990:1-1997:4 respectively. In these cases, however, we show results with lags 1 to 4 for the quadratically-detrended output gap rather than lags 1 to 4 for the labor income share as the former are more interesting. Finally, Figures 3, 9, 11, and 13 depict the graphs corresponding to figures 2, 8, 10 and 12 respectively, but with β constrained to be equal to or above 0.8 which are economically more meaningful.

The graphs show more clearly the patterns in the results that were observed from the tables. Furthermore, it is clear from the sub-sample graphs that there is evidence of parameter instabillity. In particular, whereas the quadratically-detrended output instrument set results show all parameter combinations to reject the model in the seventies, results with the same instrument set show non-rejections for the eighties and nineties.

Optimal Instrument Sets

To be able to state outcomes more specifically, one needs to rely on a particular instrument set. However, despite its desirable statistical properties, the test as presented above provides no guidance for practitioners regarding the choice of instruments. In addition, simulation studies reported in the above-cited references show that the power of AR-type tests may be affected by the number of instruments. To see this, consider the case of (5)-(6): here, the AR test requires assessing (in the regression of $\tilde{y}$ on X_1 and X_2) the exclusion of the $n \times k_2$

variables in X_2, even though the number of structural parameters under test is m (κ is $m \times 1$). On recalling that identification implies $k_2 \geq m$, we see that over-identification (or alternatively, the availability of more instruments) leads to degrees-of-freedom losses with obvious implications to power.

To circumvent these problems, Dufour-Taamouti(2003b,c) have shown that for the problem at hand, an optimal instrument (in the sense of *point-optimal* power) may be derived as follows

$$\overline{Z} = X_2 \Pi_2$$

where Π_2 is the coefficient of X_2 in the first-stage regression, *i.e.* the regression of Y on X_1 and X_2. Clearly, this strategy involves information reduction, as the associated AR-test amounts to testing for the exclusion of the $n \times m$ variables in $\overline{Z}$ and which preserves available degrees-of-freedom, even if the model is highly over-identified. In other words, the optimal test can reflect the informational content of all available instruments with no statistical costs.

Unfortunately, of course, Π_2 is unknown. So the optimal instruments needs to be estimated, with obvious implications on feasibility and exactness. Dufour(2003) shows that if the OLS estimator of Π_2 in the unrestricted reduced form multivariate regression

$$\left[\begin{array}{cc} y & Y \end{array} \right] = \left[\begin{array}{cc} X_1 & X_2 \end{array} \right] \left[\begin{array}{cc} \pi_1 & \Pi_1 \\ \pi_2 & \Pi_2 \end{array} \right] + \left[\begin{array}{cc} u & V \end{array} \right] \tag{14}$$

is used in the construction of $\overline{Z}$, then the associated AR-test coincides with the LM procedure defined by Wang-Zivot(1998). In addition, Dufour and Khalaf (2003) show that Kleibergen's K-test may be obtained as an optimal AR-test based on $\overline{Z}$ where Π_2 is replaced by it OLS estimates using the reduced form (14) constrained by the structural identification condition

$$\pi_2 = \Pi_2 \delta.$$

Dufour and Khalaf (2003) provide simple analytical formulae (applying e.g. Berndt-Savin(1977) and Dufour-Khalaf(2002b)) to derive this estimate.

Both tests so obtained are not exact, but their asymptotic validity does not impose identification away. Split sample estimation techniques (where the first sub-sample is used to estimate Π_2 and the second to run the optimal AR-test based on the latter estimate) may be easily applied to obtain exact optimal AR tests, as suggested by Dufour-Taamouti(2003b,c) and Dufour(2003); see also Dufour-Jasiak(2001) regarding split-sample procedures.

We apply the Wang-Zivot and Kleibergen equivalents of the AR test in their asymptotic and exact (split-sample case) versions to the hybrid model in equation (13). The results are found in Tables 4-7 and Figures 4-7.

In general, the obtained confidence sets for given values of ω are well-defined and fairly tight. In addition, there is a clear negative relationship between the β and θ parameters, although θ is much better identified for higher values of β. On a more detailed level, two other things become apparent: (i) the Wang-Zivot test outcomes are similar to Kleibergen's for $\omega = 0.5$ and $\omega = 0.8$, but the former yields a much smaller confidence set when $\omega = 0.2$, and (ii) the split-sample tests yield considerably smaller confidence sets than their asymptotic counterparts for $\omega = 0.2$ and $\omega = 0.5$.

The former result indicates that the use of structural information in the K-test actually yields less informative confidence sets than not using it (as in the Wang-Zivot test). However, this seems to be a characteristic of the asymptotic nature of these tests as outcomes do not differ for their split-sample (i.e., exact) counterparts. Indeed, split-sample-based confidence sets are in general more informative than their asymptotic counterparts, and clearly show that ω is actually higher than 0.6. This is an important result because it means that the hybrid NKPC is fairly well-identified for economically-reasonable values of β (i.e. values of 0.85 and higher). In this case, θ lies in the range (0.1-0.2) and ω, in the range (0.6-0.97). The implication of these results becomes apparent when the values of λ_2, γ_f and γ_b are calculated. Thus, the corresponding confidence set for the coefficient on the marginal cost coefficient is (0.02-0.47), that of the coefficient on the forward-looking component of inflation is (0.08-0.25), while the implied confidence set for the coefficient on the backward-looking component of inflation is (0.75-0.91). These decisively show that (i) firms fix prices in a preponderantly backward-looking manner, but that they adjust them almost every quarter, and (ii) not much can be learnt in the given context on the role of marginal costs for inflation.

The first outcome contrasts with conclusions of Gali-Gertler which states that firms fix their prices mainly in a forward-looking manner, but that they adjust them every 4-5 quarters. In addition, our results show that, while marginal costs are indeed significant, their importance for inflation cannot be learnt with precision; it might be that marginal costs, with a coefficient close to 0.02, plays a very small role (as in the case of the Gali-Gertler estimates), or that it plays a much larger role, with a coefficient closer to 0.5.

Conclusion

In this paper we used finite-sample methods to test the empirical relevance of the New Keynesian Phillips curve equation. In addition to traditional instrument sets, we also used optimal instruments, that were derived based on recently-developed methods. Our results were illustrated using the Gali-Gertler (1999) NKPC specifications and data, as well as a survey-based inflation expectation series from the Philadelphia Fed.

Our test rejected the reported Gali-Gertler estimates (conditional on their choice of instruments). Nevertheless, we obtained relatively informative confidence sets, specially with optimal instruments. This outcome is in contrast with those obtained by Ma (2002), and who had used Stock-Wright methods to obtain confidence sets that account for weak identification in GMM-estimated models. That is, we found the scope of the identification problem less dramatic than that suggested in Ma (2002). Indeed, our results revealed that the least-well-identified parameter is ω; namely the proportion of firms that do not adjust their prices in period t). Yet, for economically-meaningful values of the subjective discount rate, and based on the exact version of the test with optimal instruments, we concluded that firms fix prices in a predominantly backward-looking manner, adjusting prices every quarter or so. Similarly, that it is difficult to pin-point the extent to which marginal costs are important for the inflation process.

Table 1: AR test results on Gali-Gertler models - US Data

Tested model	spec.	restr	data sample	D.F.	Fstat (p-value)	Chi-stat (p-value)
Benchmark	(1)	-	70:1-97:4	88	8.77 (<)	210.54 (<)
Benchmark	(2)	-	70:1-97:4	88	9.31 (<)	223.61 (<)
Benchmark	(1)	yes	70:1-97:4	88	11.57 (<)	277.59 (<)
Benchmark	(2)	yes	70:1-97:4	88	11.55 (<)	277.27 (<)
Hybrid	(1)	-	70:1-97:4	87	7.98 (<)	199.42 (<)
Hybrid	(2)	-	70:1-97:4	87	13.55 (<)	338.83 (<)
Hybrid	(1)	yes	70:1-97:4	87	11.05 (<)	276.26 (<)
Hybrid	(2)	yes	70:1-97:4	87	17.41 (<)	435.28 (<)
Hybrid	(1)	-	70:1-89:4	55	4.73 (<)	118.21 (<)
Hybrid	(1)	yes	70:1-89:4	55	8.19 (<)	204.72 (<)
Hybrid	(2)	-	80:1-97:4	47	7.01 (<)	175.29 (<)
Hybrid	(2)	yes	80:1-97:4	47	14.13 (<)	353.19 (<)

Note: Table abreviations are: D.F. is degrees of freedom, spec is specification, restr is restricted, and the symbol " < " indicates values that are less than 10^{-5}.

Table 2: Benchmark Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Full Sample

	dw_1 - dw_4	sp_1 - sp_4	dp_1 - dp_4	s_1 - s_4	gq_1 - gq_4	dc_1 - dc_4	gc_1 - gc_4
$\theta = 0.0$	(0 - 0.8)	(0 - 1)	(0 - 0.5)	-	-	(0 - 1)	-
$\theta = 0.1$	(0.3 - 0.6)	(0.6 - 1)	(0.3 - 0.6)	-	-	(0 - 1)	-
$\theta = 0.2$	(0.5 - 0.6)	(0.7 - 1)	(0.5 - 0.6)	(0 - 0.1)	-	(0 - 1)	-
$\theta = 0.3$	0.6	(0.7 -0.9)	0.6	(0 - 0.3)	-	(0 - 1)	-
$\theta = 0.4$	0.6	(0.7 -0.8)	0.6	(0 - 0.5)	-	(0 - 1)	-
$\theta = 0.5$	0.6	(0.7 -0.8)	0.6	(0 - 0.5)	-	(0 - 1)	-
$\theta = 0.6$	0.6	(0.7 -0.8)	0.6	(0 - 0.6)	-	(0 - 1)	-
$\theta = 0.7$	0.6	(0.7 -0.8)	0.6	(0 - 0.7), 1	-	(0 - 1)	-
$\theta = 0.8$	-	(0.7 -0.8)	-	(0 - 1)	-	(0 - 1)	-
$\theta = 0.9$	-	(0.7 -0.8)	-	(0 - 1)	-	(0 - 1)	-
$\theta = 1.0$	-	(0.7 -0.8)	-	(0 - 1)	-	(0 - 1)	-

Note: Reported values are for the parameter β. Instrument sets are lags 1 to 4 of wage inflation (dw), long-short interest spread (sp), inflation (dp), labor income share (s), quadratically-detrended output gap (gq), commodity price inflation (dc), cubically-detrended output gap (gc).

Table 3a: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Full Sample

	dw_1 - dw_4										
	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
$\theta = 0.0$	(0 - 1)	-	-	-	-	-	-	-	-	-	-
$\theta = 0.1$	(0.4 - 0.7)	(0.9 - 1)	-	-	-	-	-	-	-	-	-
$\theta = 0.2$	(0.5 - 0.6)	0.8	(0.9 - 1)	-	-	-	-	-	-	-	-
$\theta = 0.3$	0.6	0.7	0.8	-	-	-	-	-	-	-	-
$\theta = 0.4$	0.6	0.7	0.7	-	-	-	-	-	-	-	-
$\theta = 0.5$	0.6	0.7	0.7	-	-	-	-	-	-	-	-
$\theta = 0.6$	0.6	-	-	-	-	-	-	-	-	-	-
$\theta = 0.7$	0.6	0.6	0.6	-	-	-	-	-	-	-	-
$\theta = 0.8$	0.6	0.6	0.6	-	-	-	-	-	-	-	-
$\theta = 0.9$	0.6	0.6	0.6	-	-	-	-	-	-	-	-
$\theta = 1.0$	-	0.6	-	-	-	-	-	-	-	-	-
	sp_1 - sp_4										
$\theta = 0.0$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.1$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.2$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.3$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.4$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.5$	-	-	-	-	0.6	-	-	-	-	-	-
$\theta = 0.6$	-	-	-	0.6	0.5	-	-	-	-	-	-
$\theta = 0.7$	-	0.6	0.6	0.6	0.5	-	-	-	-	-	-
$\theta = 0.8$	0.6	0.6	0.6	-	0.5	0.4	-	-	-	-	-
$\theta = 0.9$	0.6	0.6	0.6	0.5	-	0.4	0.3	-	-	-	-
$\theta = 1.0$	-	-	-	-	-	-	-	-	-	-	-

Note: Reported values are for the parameter β. Instrument sets are lags 1 to 4 of wage inflation (dw) and of long-short interest spread (sp).

Table 3b: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Full Sample

	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
					dp_2 - dp_5						
$\theta = 0.0$	(0-1)	-	-	-	-	-	-	-	-	-	-
$\theta = 0.1$	(0.3-0.7)	(0.8-1)	-	-	-	-	-	-	(0.7-1)	(0.3-0.5)	-
$\theta = 0.2$	(0.5-0.6)	(0.7-0.8)	(0.9-1)	1	1	(0.9-1)	(0.8-1)	(0.6-0.8)	(0.4-0.6)	0.2	-
$\theta = 0.3$	0.6	0.7	(0.7-0.8)	(0.8-0.9)	(0.7-0.9)	(0.7-0.8)	(0.6-0.7)	(0.4-0.6)	(0.3-0.4)	0.11	-
$\theta = 0.4$	0.6	0.7	0.7	0.7	(0.6-0.7)	(0.6-0.7)	(0.5-0.6)	0.4	(0.2-0.3)	0.11	-
$\theta = 0.5$	0.6	(0.6-0.7)	(0.6-0.7)	(0.6-0.7)	0.6	(0.5-0.6)	(0.4-0.5)	(0.3-0.4)	0.2	0.11	-
$\theta = 0.6$	0.6	0.6	0.6	0.6	(0.5-0.6)	(0.4-0.5)	0.4	0.3	0.2	-	-
$\theta = 0.7$	0.6	0.6	0.6	(0.5-0.6)	0.5	(0.4-0.5)	(0.3-0.4)	(0.2-0.3)	0.1	-	-
$\theta = 0.8$	-	0.6	0.6	0.5	0.5	0.4	0.3	0.2	0.1	-	-
$\theta = 0.9$	-	0.6	0.6	0.5	(0.4-0.5)	0.4	0.3	0.2	0.1	-	-
$\theta = 1.0$	-	0.6	0.6	0.5	0.4	(0.3-0.4)	0.3	0.2	0.1	-	-
					s_1 - s_4						
$\theta = 0.0$	-	-	-	-	-	-	-	-	-	0.3	0.8
$\theta = 0.1$	-	-	-	-	-	-	-	-	(0.6 - 1)	(0.1 - 0.6)	0
$\theta = 0.2$	-	-	-	-	-	1	0.9	(0.6 - 0.8)	(0.4 - 0.5)	(0.1 - 0.3)	0
$\theta = 0.3$	-	-	-	-	-	0.7	(0.6 - 0.7)	0.5	(0.3 - 0.4)	(0.1 - 0.2)	0
$\theta = 0.4$	-	-	-	0.7	0.7	0.6	0.5	0.4	(0.2-0.3)	0.1	0
$\theta = 0.5$	-	-	-	-	0.6	0.5	0.4	0.3	0.2	(0-0.1)	0
$\theta = 0.6$	-	-	0.6	0.6	-	0.5	0.4	0.3	0.2	(0-0.1)	0
$\theta = 0.7$	-	0.6	0.6	-	0.5	0.4	0.3	0.2	0.1	0	0
$\theta = 0.8$	-	0.6	0.6	-	0.5	0.4	0.3	0.2	0.1	0	0
$\theta = 0.9$	-	0.6	0.6	0.5	-	0.4	0.3	0.2	0.1	0	-
$\theta = 1.0$	-	0.6	-	0.5	-	-	0.3	0.2	0.1	0	-

Note: Reported values are for the parameter β. Instrument sets are lags lags 2 to 4 of inflation (dp) and lags 1 to 4 of labor income share (s).

Table 4: Hybrid Model - Wang-Zivot Test
Parameter Combinations that Do Not Reject H_0

	ω=0.01	ω=0.1	ω=0.19	ω=0.31	ω=0.40	ω=0.49	ω=0.61	ω=0.70	ω=0.79	ω= 0.91	ω=1.00
θ=0.01	-	-	-	-	-	-	-	-	-	-	-
θ=0.10	-	-	-	-	-	-	-	-	*(0.81-1.00)*	-	-
θ=0.19	-	-	-	-	-	*(0.99-1.00)*	*(0.81-1.00)*	*(0.64-0.99)*	(0.44-0.73)	-	-
θ=0.31	-	-	-	(0.81-0.84)	*(0.74-0.89)*	(0.67-0.87)	(0.54-0.77)	(0.41-0.64)	(0.29-0.46)	-	-
θ=0.40	-	-	-	(0.68-0.76)	(0.63-0.76)	(0.56-0.73)	(0.44-0.63)	(0.34-0.51)	(0.23-0.36)	-	-
θ=0.49	-	-	-	(0.62-0.70)	(0.56-0.68)	(0.49-0.64)	(0.38-0.53)	(0.29-0.43)	(0.20-0.30)	-	-
θ=0.61	-	-	-	(0.56-0.62)	(0.50-0.60)	(0.43-0.55)	(0.33-0.45)	(0.25-0.36)	(0.17-0.25)	-	-
θ=0.70	-	-	-	(0.54-0.60)	(0.47-0.56)	(0.40-0.51)	(0.30-0.41)	(0.22-0.32)	(0.15-0.22)	-	-
θ=0.79	-	-	-	(0.52-0.57)	(0.45-0.53)	(0.38-0.47)	(0.28-0.38)	(0.21-0.29)	(0.14-0.20)	-	-
θ=0.91	-	-	-	(0.51-0.53)	(0.43-0.49)	(0.36-0.44)	(0.26-0.34)	(0.19-0.26)	(0.13-0.17)	-	-
θ=1.00	-	-	-	(0.50-0.51)	(0.42-0.47)	(0.34-0.42)	(0.25-0.32)	(0.18-0.24)	(0.12-0.16)	-	-

ω ranges from 0.25 to 0.88.
θ ranges from 0.07 to 1.
β ranges from 0.09 to 1.

Table 5: Hybrid Model - Kleibergen Test
Parameter Combinations that Do Not Reject H_0

	ω=0.01	ω=0.1	ω=0.19	ω=0.31	ω=0.40	ω=0.49	ω=0.61	ω=0.70	ω=0.79	ω= 0.91	ω=1.00
θ=0.01	-	-	-	-	-	-	-	-	-	-	(0.01-0.21)
θ=0.10	-	-	-	-	-	-	-	-	*(0.79-1.00)*	(0.13-0.59)	(0.01-0.02)
θ=0.19	-	-	-	-	-	-	*(0.85-1.00)*	*(0.66-0.94)*	(0.43-0.69)	(0.07-0.31)	0.01
θ=0.31	-	-	(0.46-0.83)	*(0.76-0.92)*	*(0.74-0.92)*	*(0.69-0.87)*	(0.56-0.74)	(0.43-0.60)	(0.28-0.43)	(0.05-0.19)	-
θ=0.40	-	(0.65-0.73)	(0.67-0.79)	(0.66-0.81)	(0.63-0.79)	(0.57-0.73)	(0.46-0.60)	(0.35-0.48)	(0.23-0.34)	(0.04-0.15)	-
θ=0.49	(0.60-0.68)	(0.62-0.72)	(0.62-0.74)	(0.60-0.73)	(0.56-0.70)	(0.51-0.63)	(0.40-0.51)	(0.30-0.40)	(0.19-0.28)	(0.04-0.12)	-
θ=0.61	(0.60-0.69)	(0.60-0.70)	(0.59-0.70)	(0.55-0.67)	(0.51-0.62)	(0.45-0.55)	(0.35-0.43)	(0.26-0.33)	(0.17-0.23)	(0.03-0.09)	-
θ=0.70	(0.60-0.69)	(0.59-0.69)	(0.57-0.68)	(0.53-0.63)	(0.48-0.58)	(0.42-0.51)	(0.32-0.39)	(0.24-0.30)	(0.15-0.20)	(0.03-0.08)	-
θ=0.79	(0.60-0.69)	(0.59-0.68)	(0.56-0.66)	(0.51-0.60)	(0.46-0.54)	(0.39-0.47)	(0.30-0.36)	(0.22-0.27)	(0.14-0.18)	(0.03-0.07)	-
θ=0.91	(0.61-0.69)	(0.58-0.67)	(0.55-0.64)	(0.49-0.57)	(0.43-0.51)	(0.37-0.43)	(0.28-0.32)	(0.20-0.24)	(0.13-0.16)	(0.03-0.06)	-
θ=1.00	(0.61-0.69)	(0.58-0.66)	(0.54-0.62)	(0.48-0.55)	(0.42-0.49)	(0.37-0.41)	(0.27-0.30)	(0.19-0.22)	(0.12-0.15)	(0.03-0.06)	-

Table 6: Hybrid Model - Split Sample Wang-Zivot Test
Parameter Combinations that Do Not Reject H_0

	ω=0.01	ω=0.1	ω=0.19	ω=0.31	ω=0.40	ω=0.49	ω=0.61	ω=0.70	ω=0.79	ω= 0.91	ω=1.00
θ=0.01	-	-	-	-	-	-	-	-	-	*(0.01-1.00)*	(0.01-0.40)
θ=0.10	-	-	-	-	-	-	-	-	*(0.60-1.00)*	(0.01-0.53)	(0.01-0.04)
θ=0.19	-	-	-	-	-	-	*(0.77-0.86)*	(0.55-0.76)	(0.32-0.59)	(0.01-0.28)	0.01-0.02
θ=0.31	-	-	-	-	-	-	(0.48-0.59)	(0.35-0.50)	(0.21-0.37)	(0.01-0.17)	(0.01)
θ=0.40	-	-	-	-	-	(0.51-0.57)	(0.39-0.49)	(0.28-0.40)	(0.17-0.30)	(0.01-0.13)	(0.01)
θ=0.49	-	-	-	-	(0.50-0.55)	(0.43-0.51)	(0.33-0.43)	(0.24-0.34)	(0.14-0.25)	(0.01-0.11)	-
θ=0.61	-	(0.55-0.57)	(0.53-0.57)	(0.48-0.54)	(0.43-0.51)	(0.37-0.46)	(0.28-0.37)	(0.20-0.29)	(0.12-0.21)	(0.01-0.09)	-
θ=0.70	(0.54-0.58)	(0.52-0.58)	(0.50-0.56)	(0.45-0.52)	(0.40-0.48)	(0.34-0.42)	(0.25-0.33)	(0.18-0.26)	(0.11-0.18)	(0.01-0.08)	-
θ=0.79	(0.53-0.59)	(0.51-0.58)	(0.48-0.56)	(0.43-0.51)	(0.38-0.46)	(0.32-0.40)	(0.23-0.31)	(0.17-0.24)	(0.10-0.16)	(0.01-0.07)	-
θ=0.91	(0.53-0.60)	(0.50-0.58)	(0.47-0.54)	(0.41-0.49)	(0.36-0.43)	(0.30-0.37)	(0.22-0.28)	(0.15-0.22)	(0.09-0.15)	(0.01-0.06)	-
θ=1.00	(0.53-0.60)	(0.50-0.57)	(0.46-0.54)	(0.40-0.47)	(0.34-0.42)	(0.29-0.36)	(0.20-0.27)	(0.14-0.20)	(0.08-0.14)	(0.01-0.05)	-

Table 7: Hybrid Model - Split Sample Kleibergen Test
Parameter Combinations that Do Not Reject H_0

	ω=0.01	ω=0.1	ω=0.19	ω=0.31	ω=0.40	ω=0.49	ω=0.61	ω=0.70	ω=0.79	ω= 0.91	ω=1.00
θ=0.01	-	-	-	-	-	-	-	-	-	*(0.01-1.00)*	(0.01-0.57)
θ=0.10	-	-	-	-	-	-	-	-	*(0.61-1.00)*	(0.01-0.54)	(0.01-0.05)
θ=0.19	-	-	-	-	-	-	-	(0.57-0.74)	(0.33-0.58)	(0.01-0.28)	(0.01-0.03)
θ=0.31	-	-	-	-	-	-	(0.50-0.57)	(0.36-0.49)	(0.21-0.37)	(0.01-0.18)	(0.01)
θ=0.40	-	-	-	-	-	-	(0.40-0.48)	(0.29-0.40)	(0.17-0.29)	(0.01-0.14)	(0.01)
θ=0.49	-	-	-	-	-	(0.45-0.50)	(0.33-0.42)	(0.24-0.34)	(0.14-0.25)	(0.01-0.11)	(0.01)
θ=0.61	-	-	(0.54-0.55)	(0.49-0.54)	(0.44-0.50)	(0.38-0.45)	(0.28-0.36)	(0.20-0.29)	(0.12-0.20)	(0.01-0.09)	-
θ=0.70	(0.55-0.57)	(0.53-0.57)	(0.51-0.56)	(0.46-0.52)	(0.41-0.48)	(0.35-0.42)	(0.26-0.33)	(0.18-0.26)	(0.10-0.18)	(0.01-0.08)	-
θ=0.79	(0.53-0.59)	(0.51-0.58)	(0.49-0.55)	(0.43-0.50)	(0.38-0.45)	(0.32-0.40)	(0.24-0.31)	(0.17-0.24)	(0.10-0.17)	(0.01-0.07)	-
θ=0.91	(0.53-0.60)	(0.50-0.57)	(0.47-0.54)	(0.41-0.48)	(0.36-0.43)	(0.30-0.37)	(0.22-0.28)	(0.15-0.22)	(0.09-0.15)	(0.01-0.06)	-
θ=1.00	(0.53-0.60)	(0.51-0.57)	(0.46-0.53)	(0.40-0.47)	(0.34-0.42)	(0.29-0.36)	(0.20-0.27)	(0.14-0.20)	(0.08-0.14)	(0.01-0.06)	-

Figure 1: Benchmark Model - Full Sample

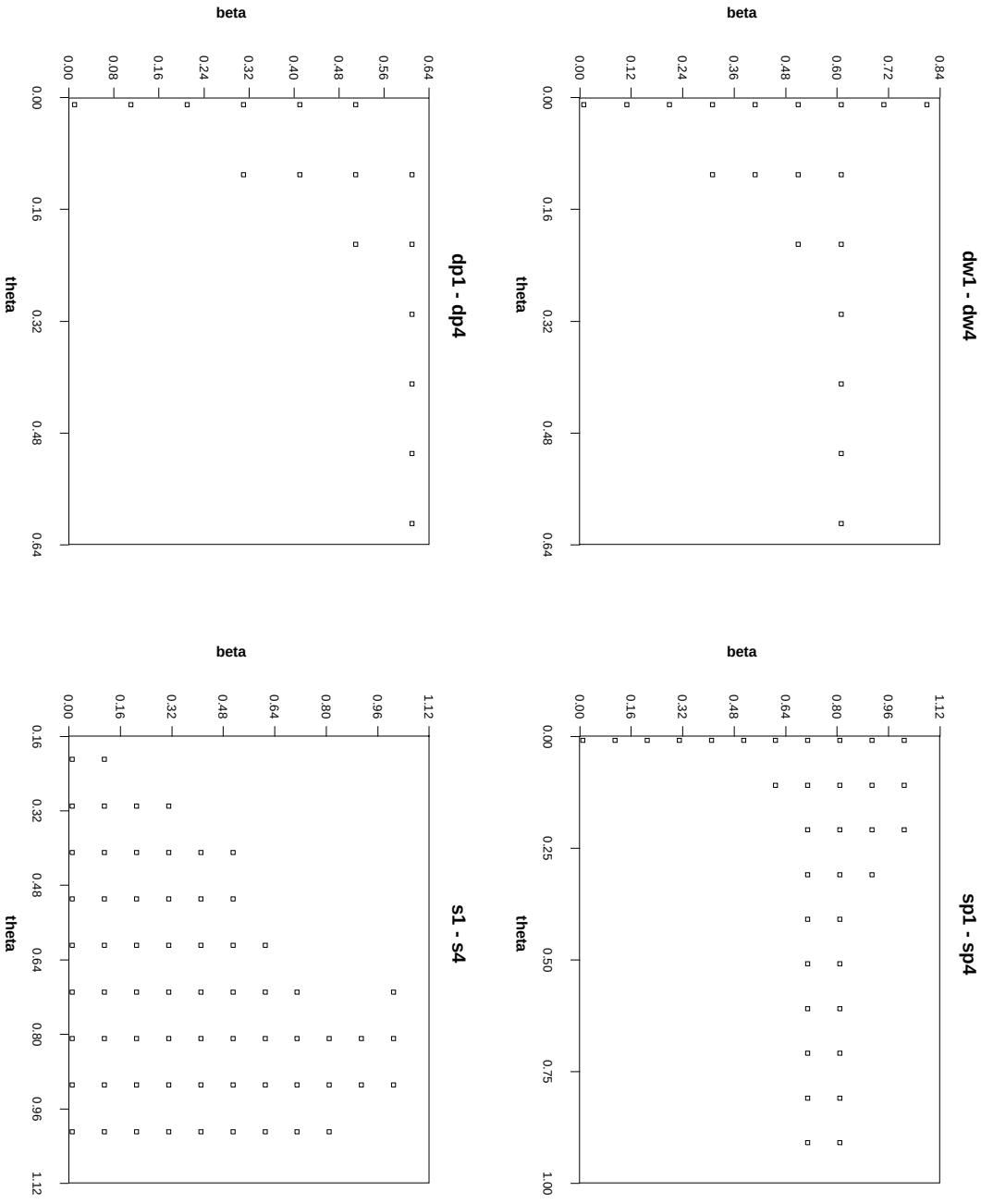


Figure 2: Hybrid Model - Full Sample

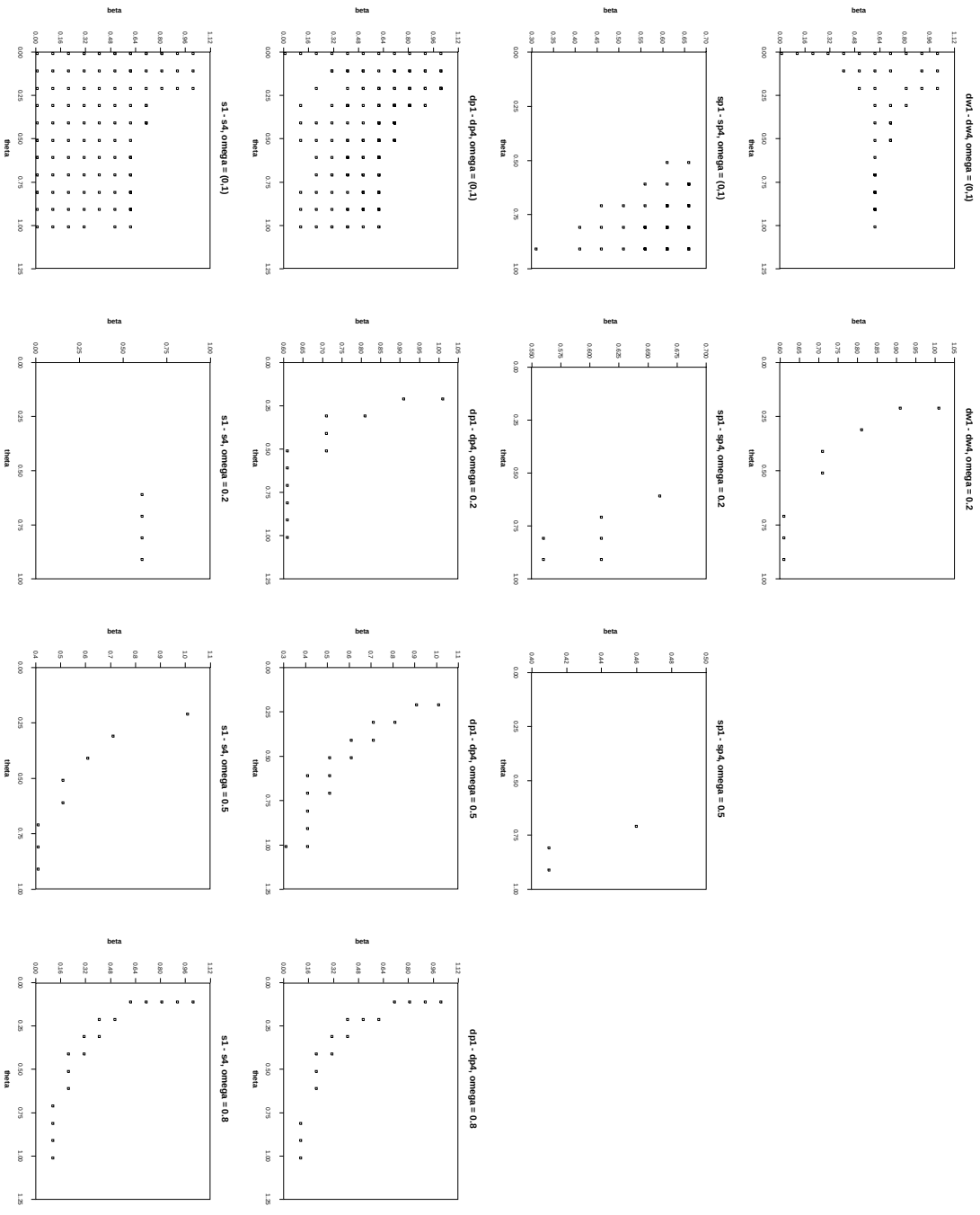


Figure 3: Constrained Hybrid Model - Full Sample
(no parameter combinations exist with the sp instruments.)

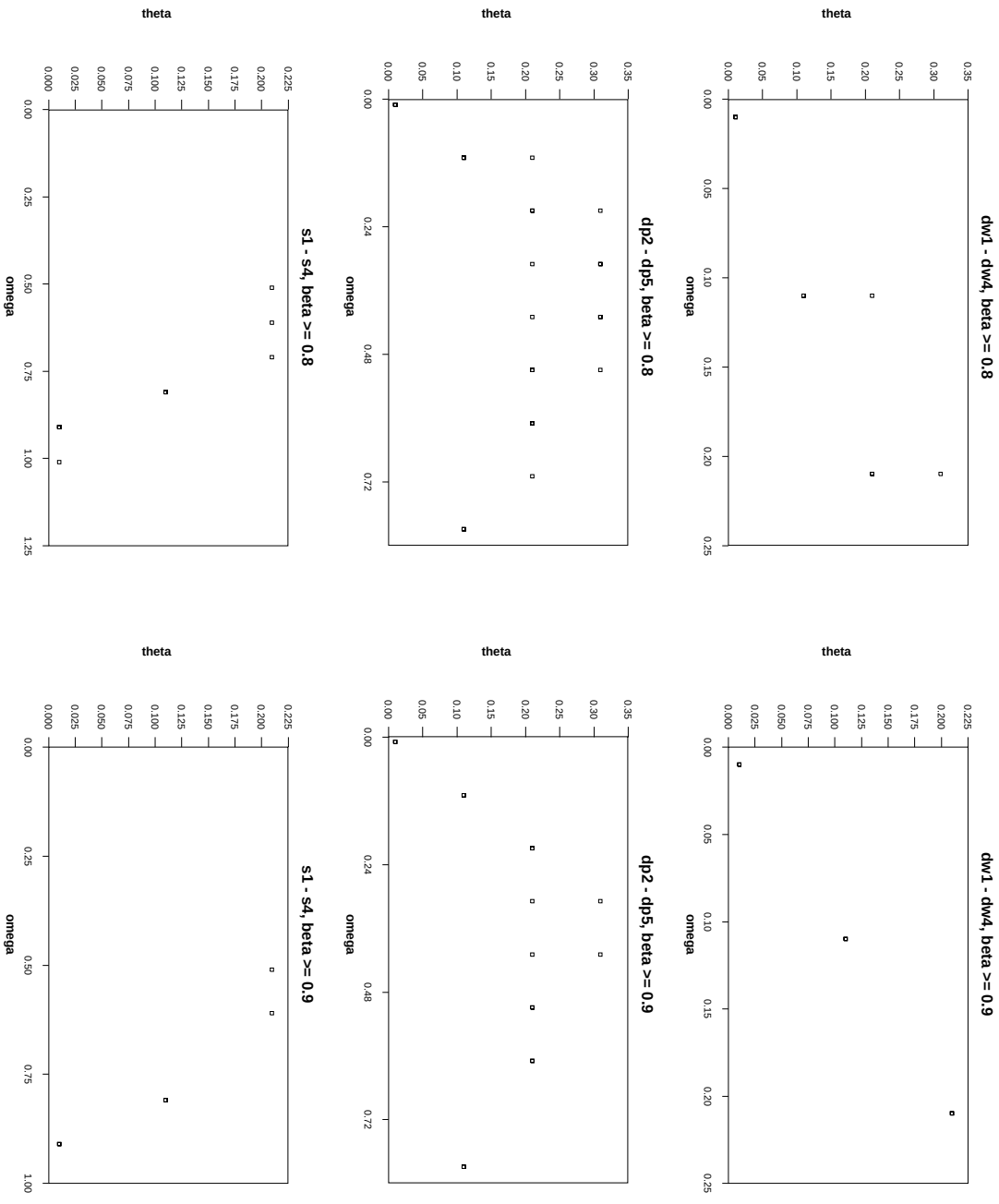


Figure 4: Wang-Zivot Test (solid line indicates $\beta = 0.85$)

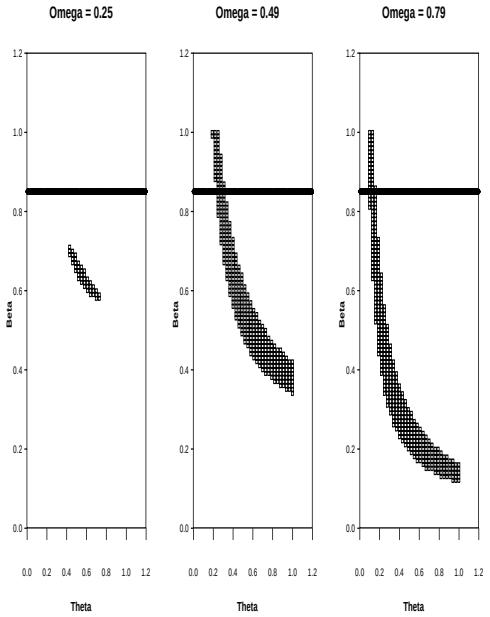


Figure 5: Kleibergen Test (solid line indicates $\beta = 0.85$)

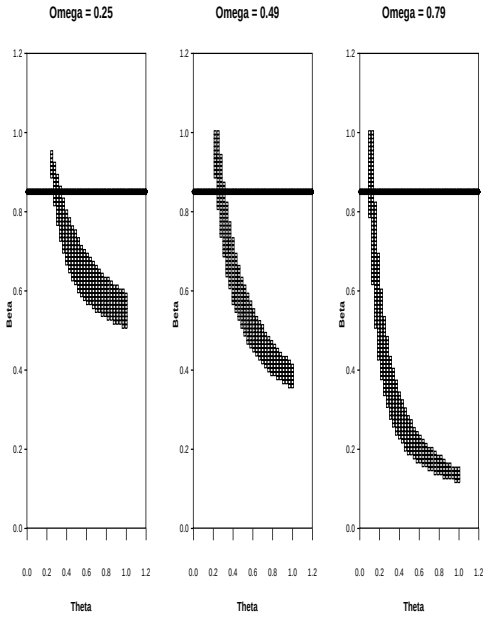


Figure 6: Split Sample Wang-Zivot Test (solid line indicates $\beta = 0.85$)

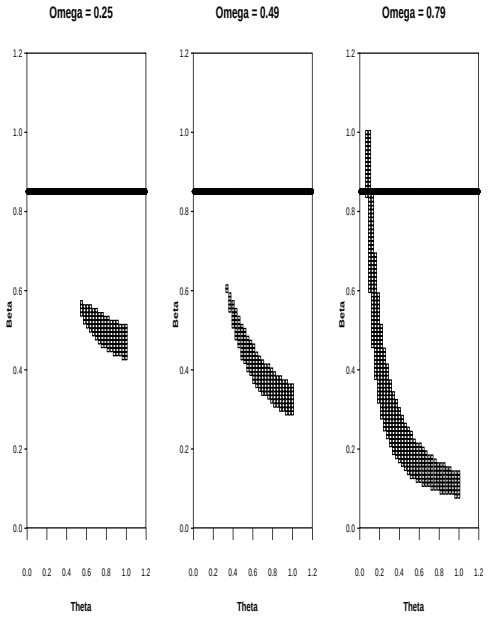


Figure 7: Split Sample Kleibergen Test (solid line indicates $\beta = 0.85$)

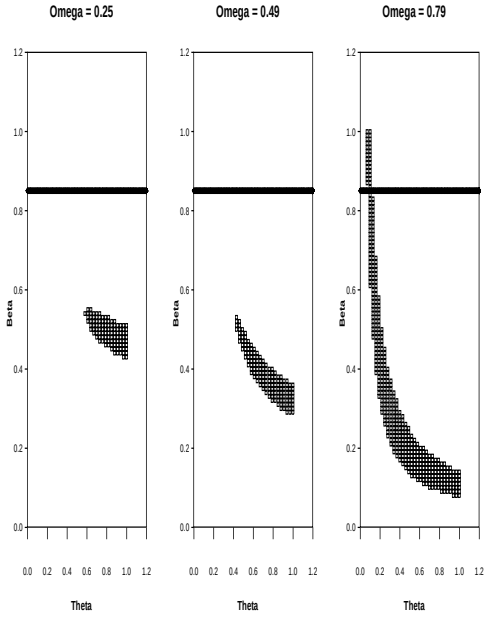


Table 8a: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Sample period (70:1 - 79:4)

	dw_1 - dw_4										
	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
$\theta = 0.0$	(0 - 1)	-	-	-	-	-	-	-	-	-	-
$\theta = 0.1$	0.8	-	-	-	-	-	-	-	-	-	-
$\theta = 0.2$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.3$	-	0.9	1	1	-	-	-	-	-	-	-
$\theta = 0.4$	0.7	0.8	(0.8 - 0.9)	0.9	0.8	-	-	-	-	-	-
$\theta = 0.5$	(0.7 - 0.8)	0.8	0.8	0.8	0.7	-	-	-	-	-	-
$\theta = 0.6$	(0.7 - 0.8)	(0.7 - 0.8)	(0.7 - 0.8)	0.7	0.7	-	-	-	-	-	-
$\theta = 0.7$	(0.7 - 0.8)	(0.7 - 0.8)	0.7	0.7	0.6	-	-	-	-	-	-
$\theta = 0.8$	(0.7 - 0.8)	(0.7 - 0.8)	0.7	(0.6 - 0.7)	0.6	0.5	-	-	-	-	-
$\theta = 0.9$	(0.7 - 0.8)	0.7	(0.6 - 0.7)	0.6	0.5	-	-	-	-	-	-
$\theta = 1.0$	(0.7 - 0.8)	0.7	(0.6 - 0.7)	0.6	0.5	0.4	-	-	-	-	-
	sp_1 - sp_4										
$\theta = 0.0$	(0-1)	-	-	-	-	-	-	-	-	-	(0-1)
$\theta = 0.1$	(0.7-0.8)	-	-	-	-	-	-	-	(0.9-1)	(0.2 - 0.7)	(0-0.1)
$\theta = 0.2$	(0.7-0.8)	(0.9-1)	-	-	-	-	1	(0.8-1)	(0.5-0.7)	(0.1-0.3)	0
$\theta = 0.3$	(0.7-0.8)	(0.8-0.9)	(0.9-1)	(0.9-1)	(0.9-1)	(0.9-1)	(0.7-0.9)	(0.5-0.7)	(0.3-0.5)	(0.1-0.2)	0
$\theta = 0.4$	(0.7-0.8)	0.8	(0.8-0.9)	(0.8-0.9)	(0.8-0.9)	(0.7-0.8)	(0.6-0.7)	(0.4-0.5)	0.3	(0.1-0.2)	0
$\theta = 0.5$	(0.7-0.8)	(0.7-0.8)	0.8	(0.7-0.8)	(0.7-0.8)	(0.6-0.7)	(0.5-0.6)	0.4	(0.2-0.3)	0.1	0
$\theta = 0.6$	(0.7-0.8)	(0.7-0.8)	(0.7-0.8)	0.7	(0.6-0.7)	(0.5-0.6)	(0.4-0.5)	(0.3-0.4)	0.2	0.1	0
$\theta = 0.7$	(0.7-0.8)	(0.7-0.8)	0.7	(0.6-0.7)	0.6	0.5	0.4	0.3	0.2	0.1	0
$\theta = 0.8$	(0.7-0.8)	0.7	0.7	(0.6-0.7)	(0.5-0.6)	0.5	0.4	0.3	0.2	0.1	0
$\theta = 0.9$	(0.7-0.8)	0.7	(0.6-0.7)	0.6	(0.5-0.6)	(0.4-0.5)	(0.3-0.4)	0.2	0.2	-	0
$\theta = 1.0$	(0.7-0.8)	0.7	(0.6-0.7)	0.6	0.5	0.4	0.3	0.2	0.1	-	0

Note: Reported values are for the parameter β. Instrument sets are lags 1 to 4 of wage inflation (dw) and of long-short interest spread (sp).

Table 8b: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Sample period (70:1 - 79:4)

	dp_2 - dp_5										
	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
$\theta = 0.0$	(0-1)	-	-	-	-	-	-	-	-	(0-1)	(0-1)
$\theta = 0.1$	0.7	-	-	-	-	-	-	(0.9-1)	(0.4-1)	(0-1)	(0-0.6)
$\theta = 0.2$	0.7	(0.9-1)	-	-	-	1	(0.8-1)	(0.5-1)	(0.2-1)	(0-0.6)	(0-0.3)
$\theta = 0.3$	0.7	(0.8-0.9)	(0.9-1)	(0.9-1)	(0.8-1)	(0.7-1)	(0.6-1)	(0.4-0.9)	(0.2-0.7)	(0-0.4)	(0-0.2)
$\theta = 0.4$	(0.7-0.8)	(0.8-0.9)	(0.8-0.9)	(0.7-1)	(0.7-1)	(0.6-0.9)	(0.5-0.8)	(0.3-0.7)	(0.1-0.5)	(0-0.3)	(0-0.1)
$\theta = 0.5$	(0.7-0.8)	(0.7-0.8)	(0.7-0.9)	(0.7-0.9)	(0.6-0.8)	(0.5-0.8)	(0.5-0.7)	(0.3-0.6)	(0.1-0.4)	(0-0.2)	(0-0.1)
$\theta = 0.6$	(0.7-0.8)	(0.7-0.8)	(0.7-0.8)	(0.6-0.8)	(0.5-0.8)	(0.5-0.7)	(0.3-0.6)	(0.2-0.5)	(0.1-0.3)	(0-0.2)	(0-0.1)
$\theta = 0.7$	(0.7-0.8)	(0.7-0.8)	(0.6-0.8)	(0.6-0.8)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.2-0.4)	(0.1-0.3)	(0-0.2)	0
$\theta = 0.8$	(0.7-0.8)	(0.7-0.8)	(0.6-0.8)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.2-0.4)	(0.1-0.3)	(0-0.1)	0
$\theta = 0.9$	(0.7-0.8)	(0.7-0.8)	(0.6-0.7)	(0.5-0.7)	(0.5-0.6)	(0.4-0.5)	(0.3-0.4)	(0.2-0.3)	(0.1-0.2)	(0-0.1)	0
$\theta = 1.0$	(0.7-0.8)	(0.6-0.7)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.3-0.4)	(0.2-0.3)	(0.1-0.2)	(0-0.1)	0
	gq_1 - gq_4										
$\theta = 0.0$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.1$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.2$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.3$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.4$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.5$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.6$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.7$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.8$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.9$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 1.0$	-	-	-	-	-	-	-	-	-	-	-

Note: Reported values are for the parameter β. Instrument sets are lags lags 2 to 4 of inflation (dp) and lags 1 to 4 of quadratically-detrended output gap (gq).

Table 9a: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Sample period (80:1 - 89:4)

	dw_1 - dw_4										
	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
$\theta = 0.0$	(0-1)	(0.5-1)	-	-	-	-	-	-	-	(0.6-1)	-
$\theta = 0.1$	(0.1-0.6)	(0.6-1)	(0.9-1)	-	-	-	1	(0.8-1)	(0.5-0.9)	(0.1-0.4)	-
$\theta = 0.2$	(0.4-0.6)	(0.5-0.7)	(0.7-0.9)	(0.7-0.9)	(0.7-1)	(0.7-0.9)	(0.6-0.8)	(0.5-0.6)	(0.3-0.4)	(0.1-0.2)	-
$\theta = 0.3$	0.5	(0.5-0.6)	(0.6-0.7)	(0.6-0.7)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.4)	(0.2-0.3)	0.1	-
$\theta = 0.4$	0.5	(0.5-0.6)	(0.5-0.6)	(0.5-0.6)	(0.5-0.6)	(0.4-0.5)	0.4	0.3	0.2	0.1	-
$\theta = 0.5$	0.5	(0.5-0.6)	(0.5-0.6)	(0.5-0.6)	(0.4-0.5)	0.4	(0.3-0.4)	(0.2-0.3)	(0.1-0.2)	-	-
$\theta = 0.6$	0.5	0.5	0.5	(0.4-0.5)	(0.4-0.5)	(0.3-0.4)	0.3	0.2	0.1	-	-
$\theta = 0.7$	0.5	0.5	0.5	(0.4-0.5)	0.4	(0.3-0.4)	0.3	0.2	0.1	-	-
$\theta = 0.8$	0.5	0.5	(0.4-0.5)	(0.4-0.5)	0.4	0.3	0.2	0.2	0.1	-	-
$\theta = 0.9$	0.5	0.5	(0.4-0.5)	0.4	(0.3-0.4)	0.3	0.2	-	0.1	-	-
$\theta = 1.0$	0.5	0.5	(0.4-0.5)	0.4	(0.3-0.4)	0.3	0.2	-	0.1	-	-
	sp_1 - sp_4										
$\theta = 0.0$	(0-1)	(0.7-1)	-	-	-	-	-	-	-	(0-1)	(0-1)
$\theta = 0.1$	(0.2-0.6)	(0.6-1)	(0.9-1)	(0.7-0.9)	(0.7-1)	-	(0.9-1)	(0.6-1)	(0.3-1)	(0-0.6)	(0-0.1)
$\theta = 0.2$	(0.4-0.6)	(0.5-0.7)	(0.6-0.9)	(0.6-0.7)	(0.5-0.7)	(0.6-1)	(0.5-0.9)	(0.4-0.7)	(0.2-0.5)	(0-0.3)	0
$\theta = 0.3$	0.5	(0.5-0.6)	(0.6-0.7)	(0.5-0.6)	(0.5-0.6)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.1-0.3)	(0-0.1)	0
$\theta = 0.4$	0.5	(0.5-0.6)	(0.5-0.6)	(0.5-0.6)	(0.4-0.5)	(0.4-0.5)	(0.3-0.5)	(0.2-0.4)	(0.1-0.3)	(0-0.1)	0
$\theta = 0.5$	0.5	(0.5-0.6)	(0.5-0.6)	(0.4-0.5)	(0.4-0.5)	(0.4-0.5)	(0.3-0.4)	(0.2-0.3)	(0.1-0.2)	(0-0.1)	0
$\theta = 0.6$	0.5	0.5	0.5	(0.4-0.5)	0.4	(0.3-0.4)	0.3	(0.2-0.3)	(0.1-0.2)	(0-0.1)	0
$\theta = 0.7$	0.5	0.5	0.5	(0.4-0.5)	(0.3-0.4)	(0.3-0.4)	(0.2-0.3)	0.2	0.1	(0-0.1)	0
$\theta = 0.8$	0.5	0.5	(0.4-0.5)	(0.4-0.5)	(0.3-0.4)	0.3	(0.2-0.3)	0.2	0.1	0	0
$\theta = 0.9$	0.5	0.5	(0.4-0.5)	0.4	(0.3-0.4)	0.3	0.2	(0.1-0.2)	0.1	0	0
$\theta = 1.0$	0.5	0.5	(0.4-0.5)	0.4	(0.3-0.4)	0.3	0.2	(0.1-0.2)	0.1	0	0

Note: Reported values are for the parameter β. Instrument sets are lags 1 to 4 of wage inflation (dw) and of long-short interest spread (sp).

Table 9b: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Sample period (80:1 - 89:4)

	dp_2 - dp_5										
	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
$\theta = 0.0$	(0-1)	(0.8-1)	-	-	-	-	-	-	-	(0.2-1)	(0-0.2)
$\theta = 0.1$	(0.2-0.6)	(0.6-7)	1	-	-	-	-	(0.8-1)	(0.5-0.9)	(0.1-0.4)	0
$\theta = 0.2$	(0.4-0.5)	0.6	(0.7-0.8)	0.8	(0.8-0.9)	(0.7-9)	(0.6-0.8)	(0.5-0.6)	(0.3-0.4)	(0-0.2)	0
$\theta = 0.3$	0.5	0.5	0.6	(0.6-0.7)	(0.6-0.7)	(0.5-0.6)	0.5	(0.3-0.4)	(0.2-0.3)	(0-0.1)	-
$\theta = 0.4$	0.5	0.5	0.6	0.6	0.5	0.5	0.4	0.3	0.2	(0-0.1)	-
$\theta = 0.5$	0.5	0.5	0.5	0.5	0.5	0.4	(0.3-0.4)	0.2	(0.1-0.2)	(0-0.1)	-
$\theta = 0.6$	0.5	0.5	0.5	0.5	0.4	0.4	0.3	0.2	0.1	0	-
$\theta = 0.7$	0.5	0.5	0.5	0.4	0.4	0.3	0.3	0.2	0.1	0	-
$\theta = 0.8$	0.5	0.5	0.5	0.4	0.4	0.3	0.2	0.2	0.1	0	-
$\theta = 0.9$	0.5	0.5	0.5	0.4	(0.3-0.4)	0.3	0.2	0.2	0.1	0	-
$\theta = 1.0$	0.5	0.5	0.5	0.4	0.3	0.3	0.2	-	0.1	0	-
	gq_1 - gq_4										
$\theta = 0.0$	-	-	-	-	-	-	-	-	-	(0 - 1)	(0 - 1)
$\theta = 0.1$	-	-	-	-	-	-	-	(0.9 - 1)	(0.4 - 0.8)	(0 - 0.5)	(0 - 0.1)
$\theta = 0.2$	-	-	-	-	-	-	-	0.5	(0.2 - 0.4)	(0 - 0.2)	0
$\theta = 0.3$	-	-	-	-	-	-	-	0.4	(0.2 - 0.3)	(0 - 0.1)	0
$\theta = 0.4$	-	-	-	-	-	-	-	0.3	0.2	(0 - 0.1)	0
$\theta = 0.5$	-	-	-	-	-	-	-	-	0.1	(0 - 0.1)	0
$\theta = 0.6$	-	-	-	-	-	-	-	0.2	0.1	0	0
$\theta = 0.7$	-	-	-	-	-	-	-	0.2	0.1	0	0
$\theta = 0.8$	-	-	-	-	-	-	-	-	0.1	0	0
$\theta = 0.9$	-	-	-	-	-	-	-	-	0.1	0	0
$\theta = 1.0$	-	-	-	-	-	-	-	-	0.1	0	0

Note: Reported values are for the parameter β. Instrument sets are lags 2 to 4 of inflation (dp) and lags 1 to 4 of quadratically-detrended output gap (gq).

Table 10a: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combinations that Do Not Reject H_0 - Sample period (90:1 - 97:4)

	dw_1 - dw_4										
	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
$\theta = 0.0$	(0-1)	(0-1)	-	-	-	-	-	-	(0-1)	(0-1)	(0-1)
$\theta = 0.1$	(0-1)	(0.5-1)	1	-	-	-	(0.9-1)	(0.4-1)	(0-1)	(0-1)	(0-0.5)
$\theta = 0.2$	(0.4-0.9)	(0.6-1)	(0.8-1)	(0.9-1)	(0.8-1)	(0.7-1)	(0.5-1)	(0.3-1)	(0-1)	(0-0.6)	(0-0.2)
$\theta = 0.3$	(0.6-0.8)	(0.7-1)	(0.7-1)	(0.7-1)	(0.7-1)	(0.5-1)	(0.4-1)	(0.2-0.9)	(0-0.7)	(0-0.4)	(0-0.1)
$\theta = 0.4$	(0.6-0.8)	(0.7-0.9)	(0.7-1)	(0.6-1)	(0.6-1)	(0.5-0.9)	(0.3-0.8)	(0.2-0.7)	(0-0.5)	(0-0.3)	(0-0.1)
$\theta = 0.5$	(0.6-0.8)	(0.6-0.9)	(0.6-0.9)	(0.6-0.9)	(0.5-0.9)	(0.4-0.8)	(0.3-0.7)	(0.1-0.6)	(0-0.4)	(0-0.2)	(0-0.1)
$\theta = 0.6$	(0.7-0.8)	(0.6-0.8)	(0.6-0.8)	(0.5-0.8)	(0.5-0.8)	(0.4-0.7)	(0.3-0.6)	(0.1-0.5)	(0-0.3)	(0-0.2)	0
$\theta = 0.7$	(0.7-0.8)	(0.6-0.8)	(0.6-0.8)	(0.5-0.8)	(0.4-0.7)	(0.3-0.6)	(0.2-0.5)	(0.1-0.4)	(0-0.3)	(0-0.2)	0
$\theta = 0.8$	(0.7-0.8)	(0.6-0.8)	(0.6-0.8)	(0.5-0.7)	(0.4-0.7)	(0.3-0.6)	(0.2-0.5)	(0.1-0.4)	(0-0.2)	(0-0.1)	0
$\theta = 0.9$	(0.7-0.8)	(0.6-0.8)	(0.6-0.8)	(0.5-0.7)	(0.4-0.6)	(0.3-0.6)	(0.2-0.4)	(0.1-0.3)	(0-0.2)	(0-0.1)	0
$\theta = 1.0$	(0.7-0.8)	(0.6-0.8)	(0.5-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.2-0.4)	(0.1-0.3)	(0-0.2)	(0-0.1)	0
	sp_1 - sp_4										
$\theta = 0.0$	(0-1)	(0.7-1)	(0.8-1)	-	-	-	-	-	(0-1)	(0-1)	(0-1)
$\theta = 0.1$	(0.3-0.8)	(0.7-1)	(0.7-1)	-	-	-	(0.8-1)	(0.3-1)	(0-1)	(0-1)	(0-0.7)
$\theta = 0.2$	(0.5-0.8)	(0.7-0.9)	(0.7-1)	(0.9-1)	(0.8-1)	(0.7-1)	(0.5-1)	(0.2-1)	(0-1)	(0-0.7)	(0-0.3)
$\theta = 0.3$	(0.6-0.8)	(0.7-0.9)	(0.7-0.9)	(0.7-1)	(0.6-1)	(0.5-1)	(0.4-1)	(0.1-1)	(0-0.7)	(0-0.4)	(0-0.2)
$\theta = 0.4$	(0.6-0.8)	(0.7-0.8)	(0.5-0.9)	(0.6-1)	(0.6-1)	(0.4-0.9)	(0.3-0.8)	(0.2-0.7)	(0-0.5)	(0-0.3)	(0-0.1)
$\theta = 0.5$	(0.6-0.8)	(0.7-0.8)	(0.6-0.8)	(0.6-0.9)	(0.5-0.8)	(0.5-0.8)	(0.3-0.7)	(0.1-0.6)	(0-0.4)	(0-0.3)	(0-0.1)
$\theta = 0.6$	(0.7-0.8)	(0.7-0.8)	(0.6-0.8)	(0.6-0.8)	(0.5-0.7)	(0.4-0.7)	(0.2-0.6)	(0.1-0.5)	(0-0.3)	(0-0.2)	(0-0.1)
$\theta = 0.7$	0.7	(0.7-0.8)	(0.6-0.7)	(0.5-0.7)	(0.4-0.7)	(0.3-0.6)	(0.2-0.5)	(0.1-0.4)	(0-0.3)	(0-0.2)	(0-0.1)
$\theta = 0.8$	0.7	(0.7-0.8)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.6)	(0.2-0.5)	(0.1-0.4)	(0-0.3)	(0-0.1)	0
$\theta = 0.9$	0.7	(0.6-0.7)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.2-0.4)	(0.1-0.3)	(0-0.2)	(0-0.1)	0
$\theta = 1.0$	0.7	(0.6-0.7)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.2-0.4)	(0.1-0.3)	(0-0.2)	(0-0.1)	0

Note: Reported values are for the parameter β. Instrument sets are lags 1 to 4 of wage inflation (dw) and of long-short interest spread (sp).

Table 10b: Hybrid Model - Parameter Grid Search Results - US Data
Parameter Combination that Do Not Reject H_0 - Sample period (90:1 - 97:4)

	$\omega = 0$	$\omega = 0.1$	$\omega = 0.2$	$\omega = 0.3$	$\omega = 0.4$	$\omega = 0.5$	$\omega = 0.6$	$\omega = 0.7$	$\omega = 0.8$	$\omega = 0.9$	$\omega = 1.0$
					dp_2 - dp_5						
$\theta = 0.0$	(0 - 1)	(0 - 1)	-	-	-	-	-	-	-	-	-
$\theta = 0.1$	(0 - 1)	(0.5 - 1)	-	-	-	-	-	-	-	-	-
$\theta = 0.2$	(0.4 - 0.8)	(0.7 - 1)	(0.9 - 1)	-	-	-	-	-	-	-	-
$\theta = 0.3$	(0.6 - 0.7)	0.8	0.9	-	-	-	-	-	-	-	-
$\theta = 0.4$	-	-	0.9	-	-	-	-	-	-	-	-
$\theta = 0.5$	-	-	0.9	-	-	-	-	-	-	-	-
$\theta = 0.6$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.7$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.8$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 0.9$	-	-	-	-	-	-	-	-	-	-	-
$\theta = 1.0$	-	-	-	-	-	-	-	-	-	-	-
					gq_1 - gq_4						
$\theta = 0.0$	-	-	-	-	-	-	-	-	-	(0-1)	(0-0.9)
$\theta = 0.1$	-	-	-	-	-	-	-	1	(0.5-1)	(0-0.7)	0
$\theta = 0.2$	-	-	1	-	1	(0.9-1)	(0.8-1)	(0.5-1)	(0.3-0.7)	(0-0.4)	0
$\theta = 0.3$	0.7	(0.8-0.9)	(0.8-1)	(0.8-1)	(0.8-1)	(0.7-1)	(0.5-0.9)	(0.4-0.7)	(0.2-0.5)	(0-0.2)	0
$\theta = 0.4$	(0.7-0.8)	(0.7-0.9)	(0.7-0.9)	(0.7-1)	(0.6-0.9)	(0.6-0.9)	(0.4-0.7)	(0.3-0.6)	(0.1-0.4)	(0-0.2)	0
$\theta = 0.5$	(0.7-0.8)	(0.7-0.8)	(0.7-0.9)	(0.6-0.9)	(0.6-0.8)	(0.5-0.7)	(0.4-0.6)	(0.2-0.5)	(0.1-0.3)	(0-0.1)	0
$\theta = 0.6$	(0.7-0.8)	(0.7-0.8)	(0.6-0.8)	(0.6-0.8)	(0.5-0.7)	(0.4-0.7)	(0.3-0.5)	(0.2-0.4)	(0.1-0.3)	(0-0.1)	0
$\theta = 0.7$	(0.7-0.8)	(0.7-0.8)	(0.6-0.8)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.2-0.4)	(0.1-0.2)	(0-0.1)	0
$\theta = 0.8$	(0.7-0.8)	(0.7-0.8)	(0.6-0.7)	(0.5-0.7)	(0.5-0.6)	(0.4-0.6)	(0.3-0.4)	(0.2-0.3)	(0.1-0.2)	(0-0.1)	-
$\theta = 0.9$	0.7	(0.6-0.7)	(0.6-0.7)	(0.5-0.7)	(0.4-0.6)	(0.3-0.5)	(0.3-0.4)	(0.2-0.3)	(0.1-0.2)	(0-0.1)	-
$\theta = 1.0$	0.7	(0.6-0.7)	(0.6-0.7)	(0.5-0.6)	(0.4-0.6)	(0.3-0.5)	(0.2-0.3)	(0.2-0.3)	(0.1-0.2)	0	-

Note: Reported values are for the parameter β. Instrument sets are lags 2 to 4 of inflation (dp) and lags 1 to 4 of quadratically-detrended output gap (gq).

Figure 8: Hybrid Model - 1970:1-1979:4
(all parameter combinations reject with the gq instruments.)

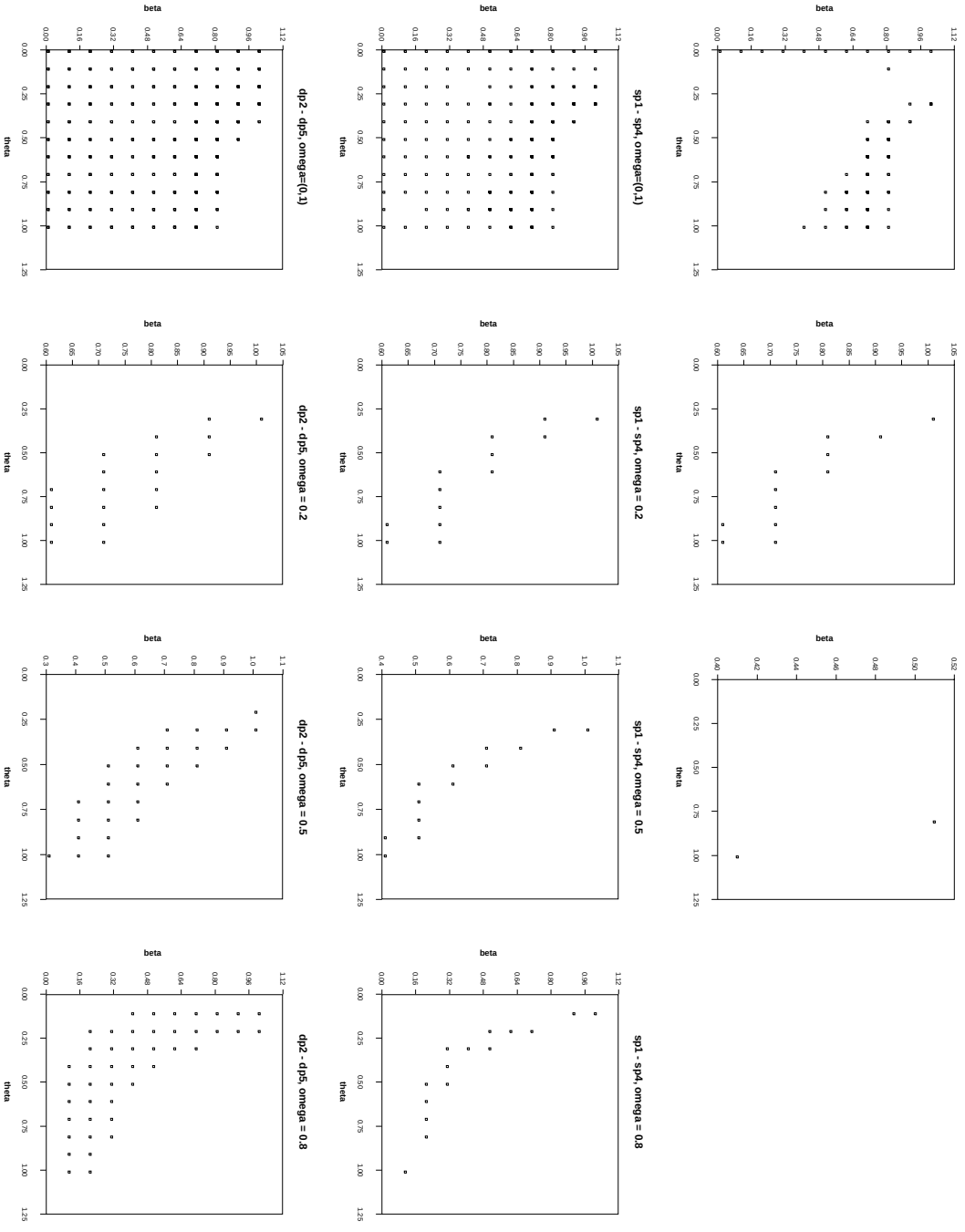


Figure 9: Constrained Hybrid Model - 1970:1-1979:4
(all parameter combinations reject with the gq instruments.)

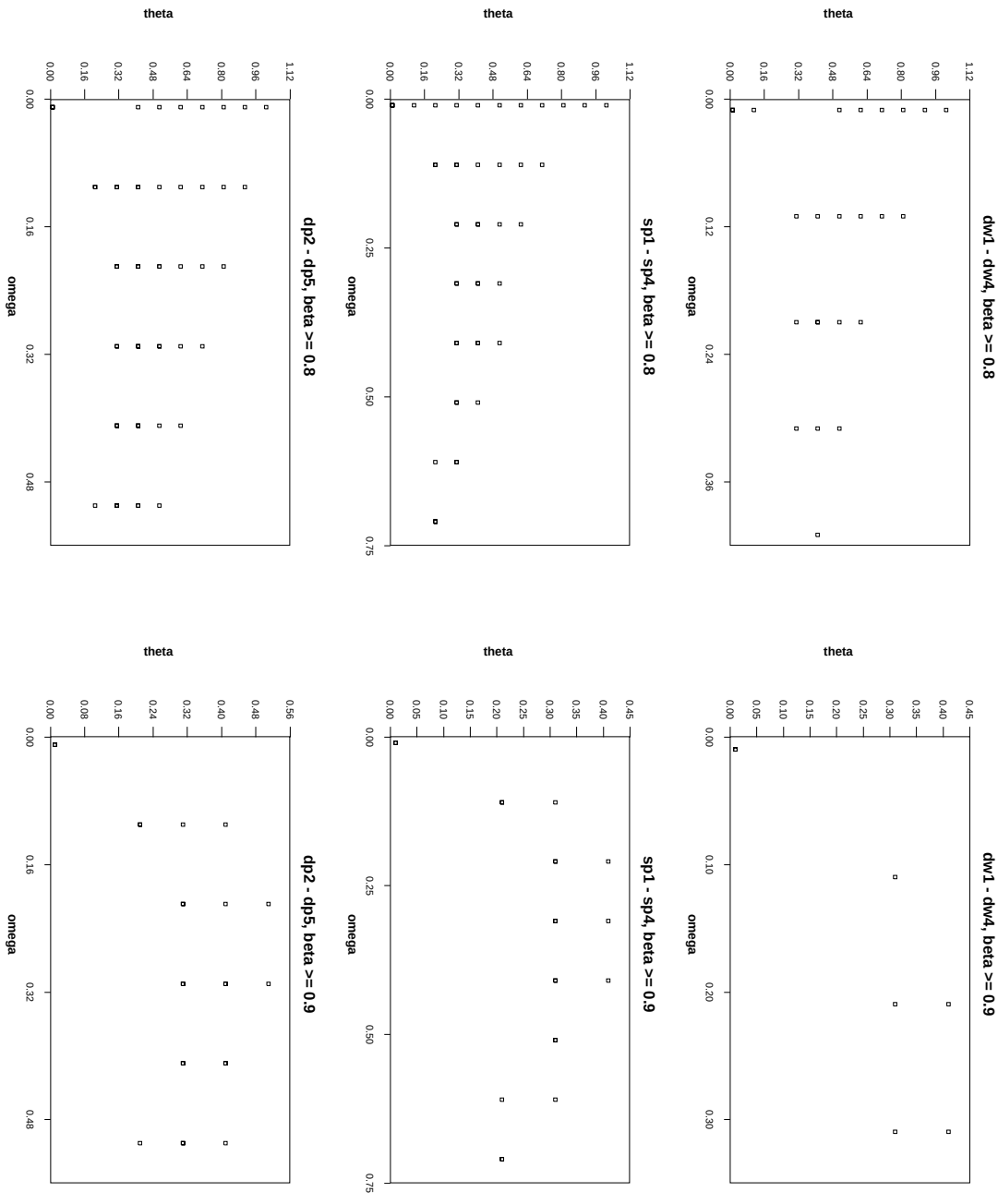


Figure 10: Hybrid Model - 1980:1-1989:4

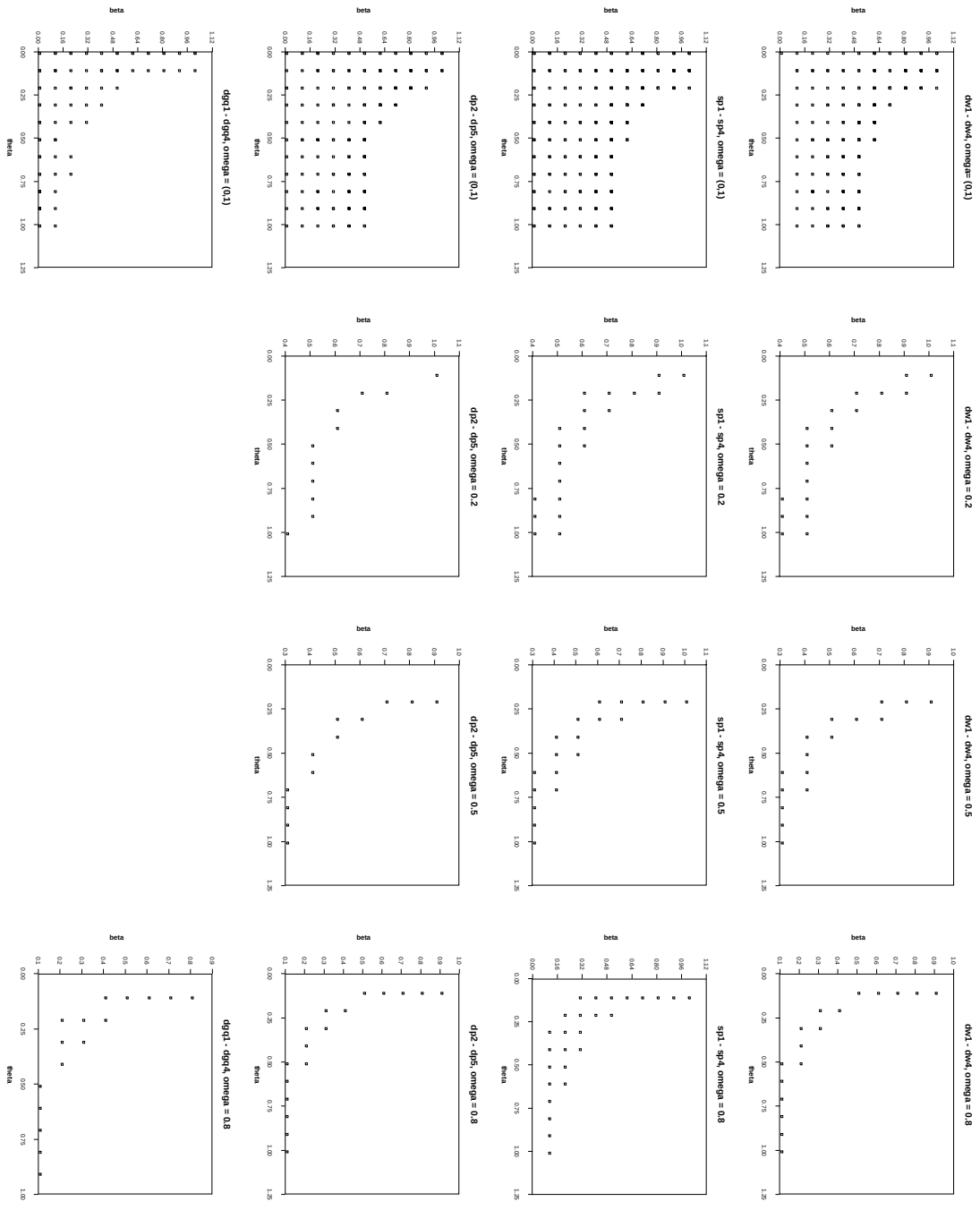


Figure 11: Constrained Hybrid Model - 1980:1-1989:4

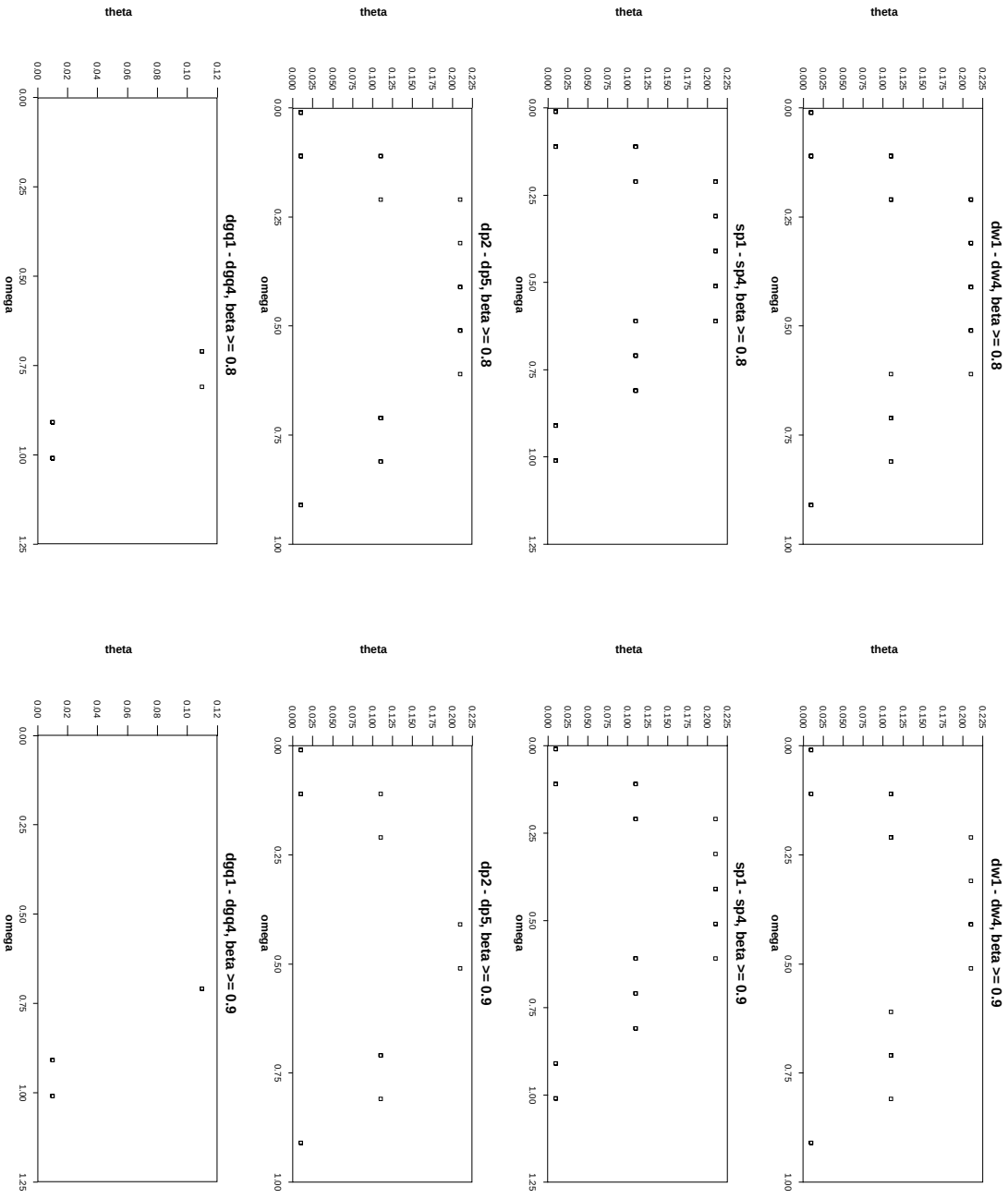


Figure 12: Hybrid Model - 1990:1-1997:4

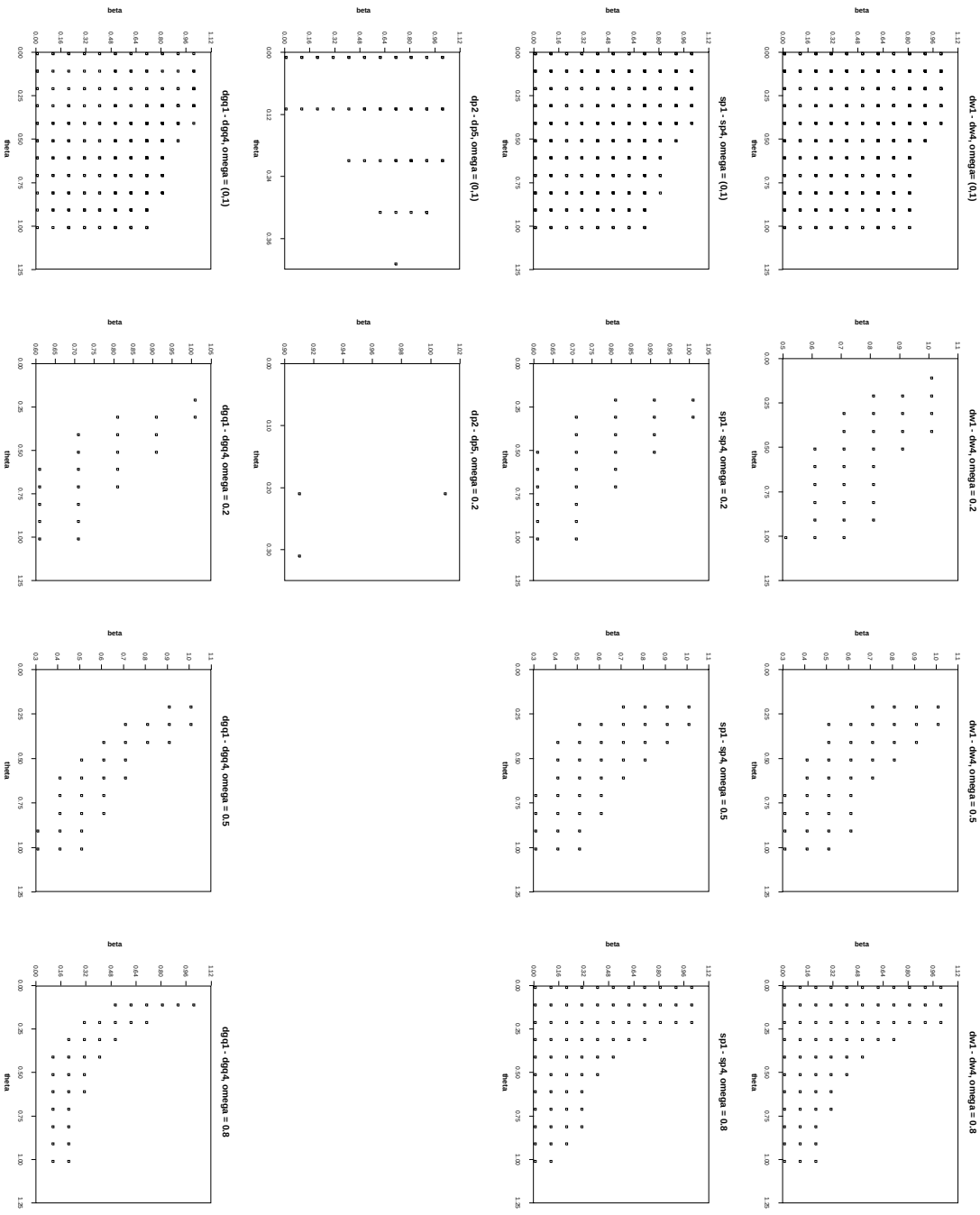
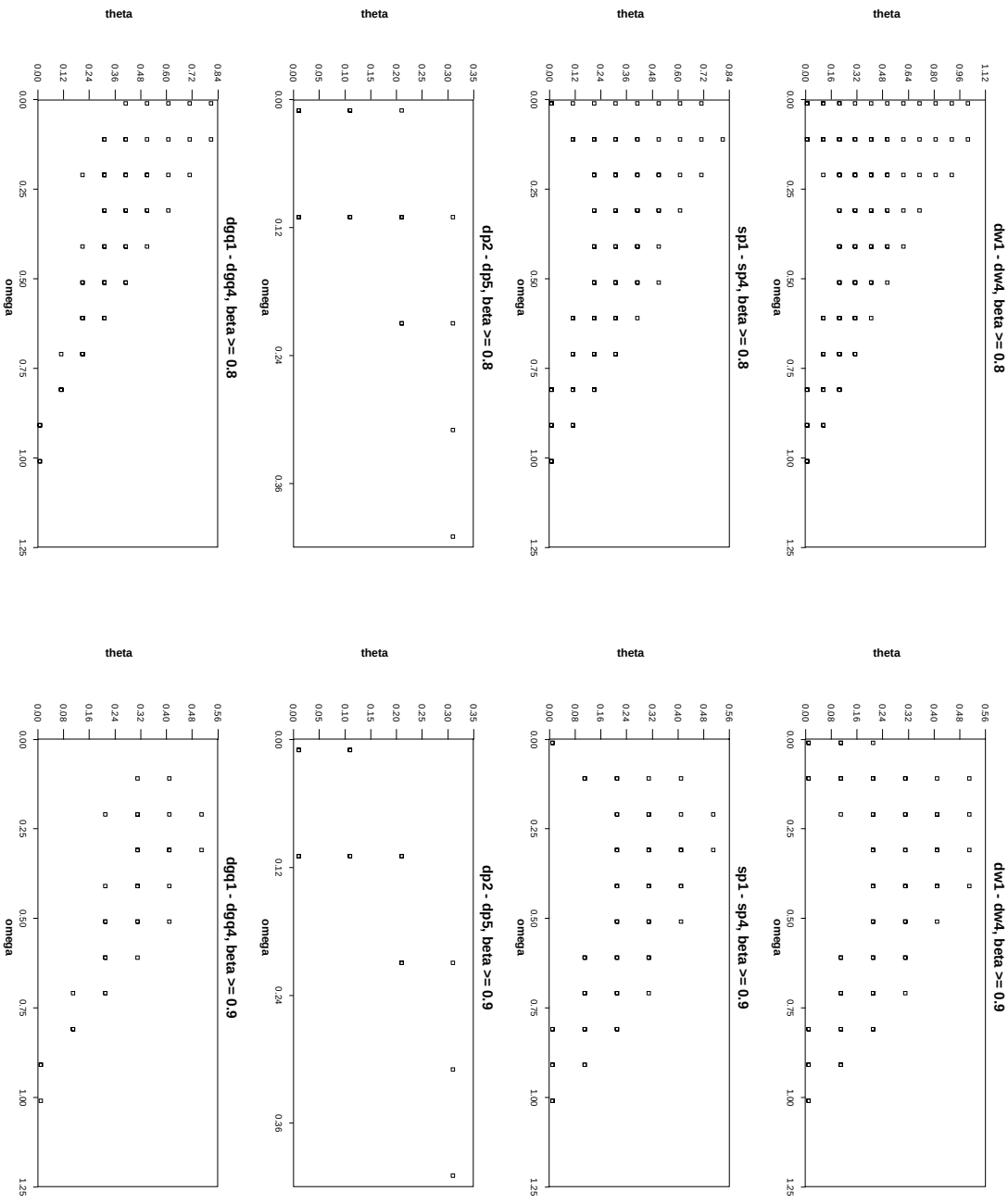


Figure 13: Constrained Hybrid Model - 1990:1-1997:4



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