## Difference-in-differences estimation using Stata

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# What is DID?

- Difference-in-differences models (DID) are used in before/after scenarios
- Examples: public policy evaluation, intervention studies
- Do increased cigarette taxes lead to a reduction in smoking?
- Simply looking at smokers who are exposed to the tax increase before and after the increase would not be enough to answer this question because there could be a general trend of reduced smoking and we could not say how much of the reduction, is attributible to the tax increase, if any
- What we also need is a group of smokers that were not exposed to the tax increase

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#### The basic idea of DID

- The basic idea of DID here is, that we can estimate the general trend of smoking from the group of non-exposed smokers, and then the difference between that and the trend among exposed smokers is the effect that can be attributed to the tax increase
- In other words, we have a before/after difference for both a treament and a control group, and then the difference between these two differences is our treatment effect, hence the name DID
- An important assumption here is that the trends are the same in both groups prior to the intervention, and that the trends would be the same in both groups had the intervention not taken place
- This is known as the parallel trends assumption. This is an effect identifying assumption, and treatment effects cannot be estimated if this assumption is violated

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#### **DID estimates ATET**



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## A simple 2x2 design

 We start with the simplest of cases where we have one treatment group, one control group, one period prior to intervention, and one period post intervention:

. list in 1/5

	id	post	treat	state	age	gender	income	ncigs
1.	1	1	0	3	58	1	60.47076	9.226687
2.	2	0	1	29	61	0	35.18789	9.694955
3.	3	1	1	49	29	0	48.33061	5.798977
4.	4	0	1	42	57	0	76.48076	4.361449
5.	5	0	1	40	40	1	65.70543	9.136448

## A simple DID model

• We estimate our first DID model using a linear model with both the treatment and pre/post variable as well as their interaction:

. regress ncio	gs i.treat##i.	post					
Source	SS	df	MS	Numk	per of obs	=	1,000
				• F(3,	996)	=	13.64
Model	591.8889	3	197.2963	Prob	5 > F	=	0.0000
Residual	14408.5533	996	14.466419	R-sc	quared	=	0.0395
				· Adj	R-squared	=	0.0366
Total	15000.4422	999	15.0154577	Root	: MSE	=	3.8035
ncigs	Coefficient	Std. err.	t	P> t	[95% co	nf.	interval]
1.treat	1928871	3442581	0.56	0.575	- 482667	3	8684415
1.post	7306656	.3352332	-2.18	0.030	-1.3885	1	0728211
.1							
treat#post							
Î 1	-1.242638	.4814626	-2.58	0.010	-2.18743	6	2978409
_cons	10.15872	.2386512	42.57	0.000	9.69040	2	10.62704

 The coefficient on the interaction term is the estimate of the difference-in-differences

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#### Cell means and DID

 More intuitively, with the simple 2x2 design, we can look at the expected outcome means for each cell:

```
. margins treat#post, post coeflegend
Adjusted predictions
                                                          Number of obs = 1,000
Model VCE: OLS
Expression: Linear prediction, predict()
                   Margin
                            Legend
  treat#post
        0 0
                 10.15872
                           b[Obn.treat#Obn.post]
        0 1
                 9.428053
                           b[Obn.treat#1.post]
        1 0
                 10.35161
                           b[1.treat#0bn.post]
        1 1
                 8.378302
                           b[1.treat#1.post]
```

Manually calculating the differences:

```
. display (_b[1.treat#1.post] - _b[1.treat#0bn.post]) - ///
> (_b[0bn.treat#1.post] - _b[0bn.treat#0bn.post])
-1.2426383
```

# Including state fixed effects to account for group level unobservables

<ul> <li>regress ncig</li> </ul>	gs i.state i.p	ost 1.trea	t#1.post				
Source	SS	df	MS	Num	ber of obs	=	1,000
				• F(5	1, 948)	=	1.86
Model	1363.45884	51	26.7344872	Pro	b > F .	=	0.0003
Residual	13636.9834	948	14.3850035	R-s	quared	=	0.0909
m-+-1	15000 4400	000	15 0154577	· Adj	R-squared	=	0.0420
IOLAL	15000.4422	999	15.01545//	ROO	L MSE	=	3./928
		0 + -1	L.		LOE8		
ncigs	Coefficient	Sta. err.	t	P> t	[95% CO	nı.	intervalj
state							
2	1.122329	1.176153	0.95	0.340	-1.18583	4	3.430493
3	2.860078	1.14564	2.50	0.013	.611794	4	5.108363
<snip< td=""><td>- &gt;</td><td></td><td></td><td></td><td></td><td></td><td></td></snip<>	- >						
50	.946973	1.175844	0.81	0.421	-1.36058	5	3.254531
1.post	7429488	.3422385	-2.17	0.030	-1.41458	2	0713161
treat#post	1 000547	4010054	0 (1	0 000	2 24007	2	2100200
1 1	-1.28354/	.4919934	-2.01	0.009	-2.24907	2	3180208
CODE	8 57291	8021031	10 69	0 000	6 99880	7	10 14701
_cons	0.37251	.0021031	10.05	0.000	0.0000	'	10.14/01

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#### Stata's DID commands

- Usually we have data with multiple pre/post observations, and treatment may be administered at different times
- Data could be repeated cross-sections or panel data
- The commands in Stata to fit DID models are didregress for repeated cross-sections, and xtdidregress for panel data
- Variety of methods for standard errors including aggregation methods, bias-corrected standard errors, and wild bootstrap
- Postestimation commands for tests and diagnostics to evaluate parallel-trends assumption

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#### Treatment as time-varying variable

 Both commands require the treatment variable to be specified as a time varying variable:

- . gen policy = treat\*post
- . list id treat post policy in 1/10, sep(0)

	id	treat	post	policy
1. 2. 3. 4. 5. 6. 7. 8. 9.	1 2 3 4 5 6 7 8 9	0 1 1 1 1 1 1 0 0	1 0 1 0 0 0 0 1 0 1 0	0 0 1 0 0 0 1 0 0 0 1 0 0 0
10.	10	1	1	1

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#### **Using** didregress

. didregress (ncigs) (policy), group(state) time(post) Number of groups and treatment time Time variable: post Control: policy = 0 Treatment: policy = 1

		Control	Treatment
Group	state	25	25
Time	Minimum Maximum	0 0	1

Difference-in-differences regression Data type: Repeated cross-sectional Number of obs = 1,000

(Std. err. adjusted for 50 clusters in state)

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ncigs	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
ATET policy (1 vs 0)	-1.283547	.5672038	-2.26	0.028	-2.423386	1437081

Note: ATET estimate adjusted for group effects and time effects.

#### The model

• We use the following (two-way fixed-effects) model:

$$\mathbf{y}_{ist} = \gamma_i + \gamma_t + \mathbf{z}_{ist}\beta + \mathbf{D}_{st}\delta + \varepsilon_{ist}$$

where:

- *y*<sub>ist</sub> is the outcome of person i in group s at time t
- $\gamma_s$  are group fixed effects
- $\gamma_t$  are time fixed effects
- zist are covariates
- $\beta$  are the coefficients on the covariates
- *D<sub>st</sub>* is the (time-varying) treatment indicator
- $\delta$  is the coefficient on the treatment indicator, i.e. the ATET
- $\varepsilon_{ist}$  are the residual errors

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#### Example with repeated cross-sections

use https://www.stata-press.com/data/r17/hospdd (Artificial hospital admission procedure data) . describe										
Contains data from https://www.stata-press.com/data/r17/hospdd.dta Observations: 7,368 Artificial hospital admission procedure data										
Variable	s:	5		7 Mar 2021 19:52						
Variable name	Storage type	Display format	Value label	Variable label						
hospital frequency month procedure satis	byte byte byte byte float	%9.0g %9.0g %8.0g %9.0g %9.0g	size mnth pol	Hospital ID Hospital visit frequency Month Admission procedure Patient satisfaction score						

Sorted by: hospital

. list in 1/5

	hospital	frequency	month	proced~e	satis
1. 2. 3. 4. 5.	1 1 1 1	High Medium Very high Medium Low	July March February April March	New Old Old New Old	4.106527 3.319475 3.41172 3.004025 3.11072

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#### DID model using didregress

. didregress (satis) (procedure), group(hospital) time(month) Number of groups and treatment time Time variable: month Control: procedure = 0 Treatment: procedure = 1

		Control	Treatment
Grou	p hospital	28	18
Time	Minimum Maximum	1	4

Difference-in-differences regression Data type: Repeated cross-sectional Number of obs = 7,368

(Std. err. adjusted for 46 clusters in hospital)

satis	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
ATET procedure (New vs Old)	.8479879	.0321121	26.41	0.000	.7833108	.912665

Note: ATET estimate adjusted for group effects and time effects.

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#### DID model using areg

. areg satis i.month i.procedure, absorb(hospital) vce(cluster hospital) Linear regression, absorbing indicators Absorbed variable: hospital F(7, 45) = 138.73

Prob > F

Root MSE

(Std. err. adjusted for 46 clusters in hospital)

R-squared

Adj R-squared

Robust satis Coefficient std. err. [95% conf. interval] t P>|t| month Februarv -.0096077 .0184317 -0.520.605 -.0467311 .0275158 .018251 1.20 0.235 -.0147907March .0219686 .0587279 0.883 April -.0032839.0221028 -0.15-.0478013.0412335 -.0094027.0232399 -0.400.688 -.0562103.0374048 Mav June -.0038375 .0190634 -0.20 0.841 -.0422332.0345581 0.629 July -.0111941.0230029 -0.49-.0575244.0351361 procedure 0.000 New .8479879 .0321121 26.41 .7833108 .912665 3.444675 .011354 303.39 0.000 3.421807 3.467543 cons

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= 0.0000

= 0.5333

= 0.5299

= 0.7238

#### Panel data

. use https://www.stata-press.com/data/r17/patents (Excerpt from Moser and Voena (2012)) . describe Contains data from https://www.stata-press.com/data/r17/patents.dta									
Observations	: 47	1,120		Excerpt from Moser and Voena (2012)					
Variables	:	5		7 Mar 2021 23:17 (_dta has notes)					
Variable name	Storage type	Display format	Value label	Variable label					
year uspatents fpatents classid gotpatent	int byte byte float byte	%9.0g %9.0g %9.0g %9.0g %9.0g	đb	Year Number of US patents Number of foreign patents Class ID Subclass got patent post 1918					

Sorted by:

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#### Panel data DID model using xtdidregress

. xtset classic	1			
Panel variable:	: classid (balanced)			
. xtdidregress	(uspatents fpatents)	(gotpatent),	group(classid)	time(year)
Number of group	os and treatment time			
Time variable:	year			
Control:	gotpatent = 0			
Treatment:	gotpatent = 1			

		Control	Treatment
Grou	p classid	6912	336
Time	Minimum Maximum	1875 1875	1919 1919

Difference-in-differences regression Data type: Longitudinal

Number of obs = 471, 120

(Std. err. adjusted for 7,248 clusters in classid)

uspatents	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
ATET gotpatent (Patent vs None)	.150516	.0356081	4.23	0.000	.0807137	.2203183

Note: ATET estimate adjusted for covariates, panel effects, and time effects.

### Small number of groups

- Sometimes the number of groups is small. For example, consider the case where cigarette taxes are raised in one state, and the control population consists of people from just two or three other states
- The default cluster-robust standard errors do not perform well when the number of clusters is small.
- didregress and xtdidregress offer three ways to deal with this issue:
  - Wild cluster bootstrap
  - bias-corrected clustered standard errors
  - Aggregated estimation with or without bias-corrected clustered standard errors

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#### Example with a small number of groups

#### Data:

. use https://www.stata-press.com/data/r17/smallg (Simulated data with a small number of groups)

. tab county

Cum.	Percent	Freq.	County
7.15 32.85 66.95 89.80 99.00 100.00	7.15 25.70 34.10 22.85 9.20 1.00	715 2,570 3,410 2,285 920 100	1 2 3 4 5 6
	100.00	10,000	Total

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#### DID model with default standard errors

. didregress (outcome x i.b) (treated), group(county) time(year) Number of groups and treatment time Time variable: year Control: treated = 0 Treatment: treated = 1

	Control	Treatment
Group county	4	2
Time Minimum Maximum	2011 2011	2013 2013

Difference-in-differences regression Data type: Repeated cross-sectional Number of obs = 10,000

(Std. err. adjusted for 6 clusters in county)

outcome	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
ATET treated (Treated vs Untreated)	- 9394987	0884134	-10 63	0 000	-1 166773	- 7122247
Note: ATET est		d for covar	iates, g	roup effe	ects, and time	effects.

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#### DID model with wild cluster bootstrap

. didregress (outcome x i.b) (treated), group(county) time(year) wildbootstrap( > rseed(123)) computing 1000 replications Confidence interval lower bound Confidence interval upper bound Number of groups and treatment time Time variable: year Control: treated = 0treated = 1Treatment . Control Treatment Group county 4 Time Minimum Maximum 2013 DID with wild-cluster bootstrap inference Number of obs = 10.000No. of clusters = Replications = 1,000 Data type: Repeated cross-sectional Error weight: rademacher Coefficient t P>|t| [96.40% conf. interval] outcome ATET treated (Treated vs Untreated) -.9394987 -10.63 0.000 -1.214059 -.6689265

Note: 96.40% confidence interval is wider than requested. Note: ATET estimate adjusted for covariates, group effects, and time effects.

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#### Parallel trends assumption

- As noted earlier, the parallel trends assumption has to hold for the ATET to be identified
- The assumption is that the trends are the same between the treatment and control groups prior to the intervention date, and that they would be the same past this date if there had not been an intervention
- It is not possible to directly test this assumption because we do not know what would have happened if there was no intervention
- A common strategy to indirectly evaluate this assumption is to check whether the trends prior to the intervention are the same, or at least similar
- The rationale here is that, if the pre-treatment trends are the same, then they would keep following these same trends in the absence of an intervention

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#### Stata commands

- Postestimation commands to assess the parallel trends assumption:
  - estat trendplots
  - estat ptrends
  - estat granger
  - estat grangerplot

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#### Graphical diagnostics

```
. use https://www.stata-press.com/data/r17/hospdd
```

(Artificial hospital admission procedure data)

- . qui didregress (satis) (procedure), group(hospital) time(month)
- . estat trendplots



Graphical diagnostics for parallel trends

#### The linear-trends model

- Let's rewrite  $y_{ist} = \gamma_i + \gamma_t + \mathbf{x}_{ist}\beta + D_{st}\delta + \varepsilon_{ist}$  as  $y_{ist} = \text{DID}_{ist} + \epsilon_{ist}$
- The linear-trends model augments the above model with two more terms:

 $y_{ist} = \text{DID}_{ist} + w_i d_{t,0} t \zeta_1 + w_i d_{t,1} t \zeta_2 + \varepsilon_{ist}$ 

- The augmentation terms consist of two 3-way interactions between d<sub>t,0</sub>, w<sub>i</sub>, and t, and d<sub>t,1</sub>, w<sub>i</sub>, and t
- $d_{t,0} = 1(d_t = 0)$  is a variable indicating pretreatment time periods
- $d_{t,1} = 1(d_t = 1)$  indicating posttreatment time periods
- *w<sub>i</sub>* variable that is 1 if ever treated, and 0 if never treated
- The coefficient ζ<sub>1</sub> captures the differences in slopes between treatment group and control group in pretreatment periods, while ζ<sub>2</sub> captures the differences in slopes in posttreatment periods.
- If ζ<sub>1</sub> is 0, the linear trends in the outcome are parallel during pretreatment periods.
- estat ptrends uses a Wald test of  $\zeta_1$  against 0 to assess whether the linear trends are parallel prior to treatment

## The Granger model

- estat granger performs a Granger-type causality test to assess whether treatment effects are observed prior to the treatment
- The Granger-type test augments the DID model with counterfactual treatment-time indicators
- The augmentation terms are referred to as leads in the DID literature
- The model used by estat granger augments the DID model with all leads (leaving out one for identification purposes):

$$y_{ist} = ext{DID}_{ist} + \sum_{j=2}^{J-1} \mathbf{1}(t_{it} \ge j) w_i \lambda_j + \nu_{ist}$$

 The test result is obtained by performing a joint Wald test on the coefficients λ<sub>j</sub>.

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#### Testing for parallel trends

```
. estat ptrends

Parallel-trends test (pretreatment time period)

H0: Linear trends are parallel

F(1, 45) = 0.55

Prob > F = 0.4615

. estat granger

Granger causality test

H0: No effect in anticipation of treatment

F(2, 45) = 0.33

Prob > F = 0.7239
```

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#### Non-parallel trends

```
. use https://www.stata-press.com/data/r17/parallelt
(Simulated data to test parallel-trends assumption)
```

- . qui xtset idl
- qui xtdidregress (y1 c.x1##c.x2) (treated1), group(id1) time(t1)
- . estat trendplots



#### Graphical diagnostics for parallel trends

#### Testing

```
. estat ptrends

Parallel-trends test (pretreatment time period)

H0: Linear trends are parallel

F(1, 199) = 39.97

Prob > F = 0.0000

. estat granger

Granger causality test

H0: No effect in anticipation of treatment

F(4, 199) = 18.17

Prob > F = 0.0000
```

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#### Nonlinear differences

- . qui xtset id2
- . qui xtdidregress (y2 c.z1##c.z2) (treated2), group(id2) time(t2)
- . estat trendplots



#### Graphical diagnostics for parallel trends

#### The Granger test is more flexible

```
. estat ptrends
Parallel-trends test (pretreatment time period)
H0: Linear trends are parallel
F(1, 999) = 2.13
Prob > F = 0.1446
. estat granger
Granger causality test
H0: No effect in anticipation of treatment
F(4, 999) = 9.86
Prob > F = 0.0000
```

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## **Time-varying effects**

- estat grangerplot fits a generalization of the DID model and plots the estimated coefficients (including their 95% confidence intervals)
- The model is similar to the Granger model above, but uses a different parameterization, and includes lags in addition to leads
- Let *I<sub>s</sub>* be the time of treatment, *m* < 0 be the number of time periods prior to *I<sub>s</sub>*, *q* ≥ 0 be the number of periods after *I<sub>s</sub>*, and *b* be the baseline period, the model is

$$egin{aligned} & \mathcal{Y}_{ist} = \gamma_i + \gamma_t + \mathbf{x}_{ist}eta + \sum_{k=m,k
eq b}^q \mathcal{B}_{st}^k w_i \lambda_k + \epsilon_{ist} \ & \mathcal{B}_{st}^k = \left\{egin{aligned} & 1(t_{it} \leq I_s + k), \, ext{if} & k = m \ & 1(t_{it} = I_s + k), \, ext{if} & m < k < q \ & 1(t_{it} \geq I_s + k), \, ext{if} & k = q \end{aligned}
ight. \end{aligned}$$

This model is also known as event-study model

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#### estat grangerplot

```
. use https://www.stata-press.com/data/r17/parallelt
(Simulated data to test parallel-trends assumption)
. xtset id2
Panel variable: id2 (balanced)
. xtdidregress (y2 c.z1##c.z2) (treated2), group(id2) time(t2)
<output omitted>
```

. estat grangerplot



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#### Numeric model results

. estat grange Fixed-effects Group variable R-squared: Within = Between = Overall = corr(u_i, Xb)	<pre>erplot, verbos (within) regr : id2 = 0.5412 = 0.6513 = 0.5342 = 0.2086</pre>	e nodraw ession (Std.	err. adju	Number Number Obs per F(21,99 Prob > usted for	of obs = of groups = group: min = avg = max = 99 = F = 1,000 cluste	10,000 1,000 10.00 466.16 0.0000 rs in id2)
у2	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
z1 z2	.8076361 0899957	.0217797 .0230564	37.08 -3.90	0.000	.7648969 1352401	.8503752 0447513
c.z1#c.z2	174932	.0359373	-4.87	0.000	2454532	1044109
2 <snir< td=""><td>0480015</td><td>.0161614</td><td>-2.97</td><td>0.003</td><td>0797157</td><td>0162874</td></snir<>	0480015	.0161614	-2.97	0.003	0797157	0162874
10	.0847351	.0159384	5.32	0.000	.0534585	.1160117
_lead5 _lead3 _lead3 _lag0 _lag1 _lag2 _lag3 _lag4 _cons	018056 .0129962 .1049961 .0515103 .2963356 .2834751 .2986596 .2727031 .3186162 7.555064	.0231218 .0221836 .0226993 .0229605 .0219243 .0222323 .0224389 .0217387 .0223891 .0181931	$\begin{array}{c} -0.78 \\ 0.59 \\ 4.63 \\ 2.24 \\ 13.52 \\ 12.75 \\ 13.31 \\ 12.54 \\ 14.23 \\ 415.27 \end{array}$	0.435 0.558 0.000 0.025 0.000 0.000 0.000 0.000 0.000 0.000 0.000	063429 0305356 .0604523 .2533126 .2398477 .2546268 .2300443 .2746811 7.519363	.0273169 .056528 .14954 .0965667 .3393587 .3271026 .3426925 .3153618 .3625514 7.590765
sigma_u sigma_e rho	.17808737 .24913922 .33816659	(fraction	of variar	ice due t	o u_i)	

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#### Granger test

. xtdidregress (y2 c.2l##c.z2) (treated2), group(id2) time(t2) Number of groups and treatment time Time variable: t2 Control: treated2 = 0 Treatment: treated2 = 1

		Control	Treatment
Grou	p id2	480	520
Time	Minimum Maximum	1	6

Difference-in-differences regression Data type: Longitudinal

Number of obs = 10,000

(Std. err. adjusted for 1,000 clusters in id2)

у2	Coefficient	Robust std. err.	t	P> t	[95% conf.	interval]
ATET treated2 (Treated vs Untreated)	.2636651	.0097188	27.13	0.000	.2445936	.2827367

Note: ATET estimate adjusted for covariates, panel effects, and time effects.

```
. estat granger
Granger causality test
H0: No effect in anticipation of treatment
F(4, 999) = 9.86
Prob > F = 0.0000
```

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# **Reproducing Granger test**

. estat grange Fixed-effects Group variable R-squared: Within = Between = Overall = corr(u_i, Xb)	<pre>erplot, post n (within) regr a: id2 = 0.5410 = 0.6513 = 0.5340 = 0.2086</pre>	odraw nlags ession (Std.	err. adju	Number Number Obs per F(17,99 Prob >	of obs = of groups = group: min = avg = max = F = 1,000 cluste	10,000 1,000 10.0 573.04 0.0000 rs in id2)
		Robust	_			
y2	Coefficient	std. err.	t	P> t	[95% conf.	interval]
z1 z2	.8078464 0899448	.0217724 .0230523	37.10 -3.90	0.000	.7651215 1351811	.8505714 0447084
c.zl#c.z2	1750781	.035931	-4.87	0.000	2455871	1045692
t2 2 <spir< td=""><td>0480031</td><td>.0161587</td><td>-2.97</td><td>0.003</td><td>0797119</td><td>0162942</td></spir<>	0480031	.0161587	-2.97	0.003	0797119	0162942
10	.0975545	.0142977	6.82	0.000	.0694975	.1256114
_lead5 _lead4 _lead3 _lead2 _lag0 _cons	0180553 .0129911 .1049946 .0515093 .2939576 7.554972	.0231174 .0221788 .0226945 .0229561 .0170635 .0181973	-0.78 0.59 4.63 2.24 17.23 415.17	0.435 0.558 0.000 0.025 0.000 0.000	0634195 0305313 .0604603 .0064615 .2604733 7.519263	.0273089 .0565136 .1495289 .096557 .3274419 7.590681
sigma_u sigma_e rho	.17808747 .24915053 .33814654	(fraction	of variar	ice due t	:o u_i)	
. test _lead2 (1) _lead2 (2) _lead3 (3) _lead4 (4) _lead4 F(4,)	_lead3 _lead4 = 0 = 0 = 0 = 0 999) = 9 cob > F = 0	_lead5 .86 .0000			< • >	

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# Reproducing ATET

. xtdidregress (y2 c.zl##c.z2) (treated2), group(id2) time(t2) Difference-in-differences regression Number of obs = 10,000 Data type: Longitudinal

(Std. err. adjusted for 1,000 clusters in id2)

v2	Coefficient	Robust std. err.	t	P>ItI	[95% conf.	intervall
ATET treated2 (Treated vs Untreated)	.2636651	.0097188	27.13	0.000	.2445936	.2827367
Note: ATET est . estat grang. Fixed-effects Group variable R-squared: Within Between Overall : corr(u_i, Xb)	<pre>timate adjuste erplot, verbos (within) regr e: id2 = 0.5390 = 0.5931 = 0.5097 = 0.1818</pre>	d for covar e nodraw nl ession (Std.	err. adj	anel effe nlags(0) Number Number Obs per F(13,99 Prob > usted for	ects, and time of obs = of groups = group: min = avg = max = ef = 1,000 cluste	effects. 10,000 1,000 10 10.0 744.05 0.0000 rs in id2)
	Coefficient	Robust	+	Polti	[95% conf	intervall
21 22	.80816 0894164	.021798	37.07	0.000	.7653848	.8509351 0440338
c.zl#c.z2 t2 2 <snij 10</snij 	1751386 031873 p> .1227044	.0360169 .0110175 .0122365	-4.86 -2.89 10.03	0.000	2458161 0534932 .0986921	104461 0102528 .1467167
_lag0 _cons	.2636651 7.545177	.0097188	27.13 577.49	0.000	.2445936 7.519538	.2827367 7.570816
sigma_u sigma_e rho	.18910858 .2496288 .36463394	(fraction	of varia	nce due t	:o u_i)	
						Image: 1

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#### **Final remarks**

- didregress and xtdidregress implement the TWFE DID estimator
- Also fits triple-difference models (DDD)
- https://www.stata.com/manuals/tedidregress.pdf
- didregress and xtdidregress can handle multiple treatment times, but TWFE DID can be problematic due to timing effects (see Goodman-Bacon 2021; ssc describe bacondecomp)
- DID is a fast growing literature, e.g.:
  - Nonlinear DID (Wooldridge 2021)
  - Doubly-robust DID (Sant'Anna & Zhao 2020)
  - Heterogenous DID (Callaway & Sant'Anna 2021; De Chaisemartin & D'Haultfoeuille 2022)

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Thank you!

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