

# Estimation of two-stage models in individual participant data with (or without) missing data

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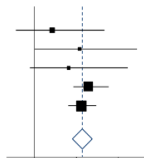


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- IPD Meta-analysis (IPDMA)
- `twostage`
- Motivating example: TPC study
- `twostage_post`
- Missing data in IPDMA using `twostage`
- Final remarks

# Individual Participant Data Meta Analysis (IPDMA)

- Use of **raw data** from studies.
- Investigate more granule effects such as **treatment covariate interactions** and/or **joint effects**.
- Ensures that similar or **same model** is fitted in all studies.
- Ensures that **relevant participants** are included.
- Overcome **methodological challenges** such as missing data.
- **Two-stage approach**: 1. Fit the model in each study individually. 2. Combine the estimates from the study.



Available options for two-stage IPDMA in Stata:

- 1 `mymeta` (Ian White), 2009
- 2 `ipdmetan` (David Fisher), 2013

```
use "ipddata.dta", clear
stset t, fail(failure)
```

### **mvmeta**

```
mvmeta_make stcox trt, strata(sex) by(trialid) ///
names(b V) clear
mvmeta b V, reml
```

### **idpmetan**

```
idpmetan, study(trialid) re(reml) poolvar(trt) nograph:
///
stcox trt, strata(sex)
```

### **twostage**

```
twostage stcox trt, strata(sex) id(trialid) mv(reml)
```

# twostage: facilitating multivariate IPDMA

**twostage** *command varlist* [if] [in], [cmd options] **[options]**

- twostage works with **official** and **user-written** commands.
- Use of **meta mvregress** for **multivariate IPDMA**.
- Allows for new **factor notations** **i.** and **#**.
- Allows to be used with **mi estimate**.
- **frames** to allow user to access study specific estimates.
- Access command-specific post-estimation commands.
- Integration of **twostage\_postest** for **post estimation commands**: use with `lincom`, `test`, visualisation.

# Motivating example: TPC study

## Training Performance in Cycling (TPC) study



The aim of the study is to assess the joint effect between different training methods and levels of altitude on performance in professional cyclists.

# Motivating example: TPC study

- Observational study with around 2000 participants per study and 5 study sites.
- **Training methods:** Aerobic training, VO2 max training, and threshold oriented training.
- **Training altitude:**

$< 1000, 1000 - 1800m, > 1800m$

- **Outcome:** Placing in top 5 in professional races (yes/no).
- A single study would have **low power** to detect any joint effects of training method and altitude. **Pooled estimates** from 5 study locations increase statistical power.



# Motivating example: TPC study

```
tabulate altitude method
```

altitude	Aerobic	V02	Threshold	Total
<1000	1,535	1,137	1,768	4,440
1000-1800	1,048	795	1,207	3,050
>1800	901	632	977	2,510
Total	3,484	2,564	3,952	10,000

We are interested in the **joint effect** of **different levels** of **altitude** and **training methods**.

# Outcome model with indicator variables

$$\begin{aligned} \text{logit}(P(\text{Winning} = 1 | \text{Training Method, Altitude})) = \\ \beta_0 + \beta_1 \text{vo2} + \beta_2 \text{thres} + \beta_3 \text{med\_alt} + \\ \beta_4 \text{high\_alt} + \beta_5 \text{vo2\_med\_alt} + \beta_6 \text{vo2\_high\_alt} + \\ \beta_7 \text{thres\_med\_alt} + \beta_8 \text{thres\_high\_alt} \end{aligned}$$

# Facilitating twostage

```
use tpc.dta, clear
```

```
twostage logit winning vo2 thres med_alt high_alt ///  
vo2_med_alt vo2_high_alt thres_med_alt thres_high_alt, ///  
id(id) frm(tpc_study_est)
```

```
// Alternatively
```

```
twostage logit winning i.meth##i.alt, id(id) frm(tpc_study_est)
```

twostage gives the following output with the pooled estimates from all variables:

Two-stage IPD meta-analysis

Number of studies: 5

Number of participants: 10000

```
-----+-----
```

	Coefficient	Std. err.	z	P> z	[95% conf. interval]	
winning						
vo2	.053065	.128468	0.41	0.680	-.1987278	.3048577
thres	.2261234	.1111222	2.03	0.042	.0083278	.443919
med_alt	.1243019	.1290233	0.96	0.335	-.1285792	.3771829
high_alt	.0954654	.1377031	0.69	0.488	-.1744277	.3653586
vo2_med_alt	.4137719	.1869495	2.21	0.027	.0473576	.7801862
vo2_high_alt	.7736476	.1939756	3.99	0.000	.3934625	1.153833
thres_med_alt	.7589502	.1619021	4.69	0.000	.4416278	1.076273
thres_high_alt	1.030928	.1703431	6.05	0.000	.6970621	1.364795
_cons	-2.171521	.0845473	-25.68	0.000	-2.337231	-2.005812

```
-----+-----
```

Study-specific estimates and SE are saved in a frame.

**frame tpc\_study\_est: summarize**

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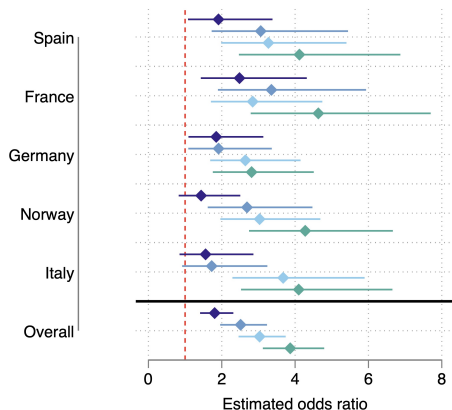
**twostage\_post** offers post estimation commands for twostage. To get linear combinations for the four joint effects of interest we can type:

```
twostage_post ///
    (vo2 + med_alt + vo2_med_alt) ///
    (vo2 + high_alt + vo2_high_alt) ///
    (thres + med_alt + thres_med_alt) ///
    (thres + high_alt + thres_high_alt) , ///
    eform graph
```

Twostage post estimation

Linear Combination of vo2 + med\_alt + vo2\_med\_alt

	Coef	SE	p-val	LB	UB
-----+-----					
Spain	1.911	0.557	0.026	1.079	3.383
France	2.483	0.701	0.001	1.428	4.319
Germany	1.849	0.498	0.022	1.091	3.134
Norway	1.437	0.407	0.200	0.825	2.505
Italy	1.559	0.483	0.152	0.849	2.863
-----+-----					
Overall	1.806	0.229	0.000	1.408	2.316



- ◆ Joint effect between V02 and medium altitude
- ◆ Joint effect between V02 and high altitude
- ◆ Joint effect between Threshold and medium altitude
- ◆ Joint effect between Threshold and high altitude



With the provided results we can build the final table:

**Table 1:** Overall joint effects between training method and levels of altitude on cycling performance.

Training  Altitude	Training Method		
	Aerobic	V02	Threshold
-----+-----			
<1000	ref.	1.05(0.82,1.36)	1.25(1.01,1.59)
1000-1800	1.13(0.88,1.46)	1.81(1.40,2.32)	3.03(2.46,3.74)
>1800	1.10(0.84,1.44)	2.51(1.96,3.23)	3.87(3.12,4.79)

## Conclusion

**Threshold** training at **medium** and **high altitude** is the most effective training to win cycling races.

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- Systematically missing data in IPDMA can pose **practical** and **methodological** challenges for researchers.
- Multiple imputation can be used to **learn** from other studies and impute values for systematically missing data.
- `mi estimate` currently has no two-stage command.
- `mvmeta` and `ipdmetan` can be used with prefix.

# Integration into **mi** environment

Let us assume we have some sporadically missing data.

```
use tpcdata.dta, clear
```

```
replace altitude = . if runiform()<.4
```

```
mi set wide  
(...)
```

```
mi impute mlogit altitude vo2 thres winning vo2_win thres_win, by(id) add(40)  
(...)
```

```
mi estimate, dots post: ///  
twostage logit winning vo2 thres med_alt high_alt ///  
vo2_med_alt vo2_high_alt thres_med_alt thres_high_alt, ///  
id(id) frm(tpc_mi_est)
```

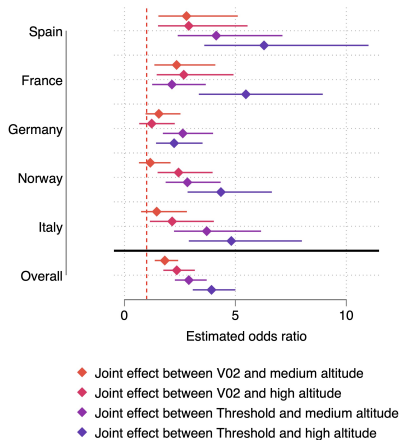
# twostage and mi

```
Multiple-imputation estimates          Imputations      =      40
Two-stage IPD meta-analysis          Number of obs    =    10,000
                                      Average RVI      =     0.3824
                                      Largest FMI     =     0.3606
DF adjustment:   Large sample        DF:      min    =     306.92
                                      avg          =     623.63
                                      max          =    1,425.27
Model F test:      Equal FMI         F(   8, 3417.4) =     31.18
                                      Prob > F      =     0.0000
```

```
-----
      | Coefficient  Std. err.   t    P>|t|   [95% conf. interval]
-----+-----
      vo2 | .0270338   .1502546   0.18  0.857   -.2680766   .3221441
      thres | .1634354   .1261954   1.30  0.196   -.0842159   .4110867
      med_alt | .0057517   .1560645   0.04  0.971   -.3009186   .3124222
      high_alt | .1081341   .1564237   0.69  0.490   -.1990948   .4153631
      vo2_med_alt | .5649013   .2291951   2.46  0.014   .1142125   1.01559
      vo2_high_alt | .7226173   .2404113   3.01  0.003   .2495543   1.19568
      thres_med_alt | .8962267   .1974459   4.54  0.000   .5081353   1.284318
      thres_high_alt | 1.095521   .1980394   5.53  0.000   .7064293   1.484612
      _cons | -2.139291   .093498   -22.88  0.000   -2.322699   -1.955882
-----
```

# twostage and mi

We can use `twostage_post` again to initiate overall and study specific linear combinations and visualisations.



**Table 1:** Overall joint effects between training method and levels of altitude on cycling performance.

Training  Altitude	Training Method		
	Aerobic	V02	Threshold
-----+-----			
<1000	ref.	1.02(0.78,1.38)	1.17(0.92,1.51)
1000-1800	1.01(0.74,1.36)	1.82(1.37,2.42)	2.90(2.27,3.71)
>1800	1.11(0.82,1.51)	2.36(1.75,3.17)	3.92(3.08,5.00)

## Conclusion

No change in the overall conclusion. The values after MI are close to the set parameters.

- twostage offers flexible ways to estimate **two-stage models for multivariate IPDMA**.
- Possibility for users compute a range of **post estimation commands** with `twostage_post`.
- Integration into the **mi environment**.
- Useful alternative and extension to established commands `mvmeta` and `ipdmetan`.



# Further readings



Fisher DJ. *Two-stage individual participant data meta-analysis and generalized forest plots*. *Stata Journal* 2015;15(2):369-96



Jolani S, Debray TPA, Koffijberg H, va Buuren S, Moons KGM. *Multiple imputation of systematically missing predictors in an individual participant data meta-analysis: a generalised approach using MICE*. *Stat Med* 2015; 34(11):1841-1863.



Morris TP, Fisher DJ, Kenward MG, Carpenter JR. *Meta-analysis of Gaussian individual patient data: Two-stage or not two-stage?* *Stat Med*, 2018; 37(9):1419-1438.



Resche-Rigon M, White IR, Bartlett JW, Peters SA, Thompson SG. *Multiple imputation for handling systematically missing confounders in meta-analysis of individual participant data*. *Stat Med* 2013; 32(28):4890-4905.



Riley RD, Tierney J, Stewart LA (Eds). *Individual Participant Data Meta-Analysis: A Handbook for Healthcare Research*. Chichester: Wiley, 2021.



Riley RD, et al. *Multivariate meta-analysis using individual participant data*. *Res Synth Method*. 2015; 6 157-74.



White, I. R. *Multivariate Random-effects Meta-analysis*. *Stata Journal* 2009;9(1): 40–56.



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Joint work with Nicola Orsini.