An Integrated Approach For Stock Price Forecasting

Gustavo Santos Raposo  
Department of Electrical Engineering, Pontifical Catholic University of Rio de Janeiro

Alvaro Veiga  
Department of Electrical Engineering, Pontifical Catholic University of Rio de Janeiro

October 17, 2004

Draft Version

Abstract

This article faces the problem of stock price forecasting through an integrated approach in which the modeling of high frequency financial data (duration, volume and bid-ask spread) uses a contemporaneous ordered probit model. Here, the formulation introduced by Raposo and Veiga (2004) – EMACM – is used in order to capture the dynamic that high frequency variables present, and its forecasting function is taken as proxy to the contemporaneous information necessary to the price model. In that context, the main purpose of the article is to test the performance of the proposed model and compare it with the results obtained based on a NAIVE rule.

Keywords: High frequency data, ordered probit model, EMACM, nonlinear time series.
1 Introduction

The challenge of understanding market price dynamics has been enforced by recent technological developments. Nowadays, with the existence of “high frequency” database, it’s possible to understand the microstructures dynamics and asset price behaviors. Here, the question is how the environment (negotiation systems and investors) could influence asset market price, bearing in mind that, in the real world, financial market imperfections exists and, in reality, are investigated and considered by the participants.

Among the objectives of that paper, could be pointed:

- Understand and model the dynamic of high frequency data, in particular: duration, volume and spread;
- Model the price-making process measuring the influence of the microstructures – asset price changes distribution and understand the rationality behind buy and sell orders;
- Analyze the evidences of forecasting capability regarding financial asset prices.

That article is divided as follows. Section 2 presents the EMACM and Ordered Probit Model formulation. Section 3 brings an empirical example and, finally, Section 4 concludes.

2 The Model

In order to model the dynamic behind the microstructures, that article uses the methodology introduced by Raposo and Veiga (2004) – EMACM. That formulation is appropriated due to the capability to deal with causality among variables and the forecasting function that can be directly used in the ordered probit formulation, providing price change estimation.

2.1 EMACM:

A set of high-frequency variables (duration – \(x_i\), volume – \(\nu_i\) and bid-ask spread – \(s_i\)) follows an Exponential Multivariate Autoregressive Conditional High Frequency Data Model (EMACM), if:

\[
\begin{align*}
    x_i &= \psi_i \cdot \varepsilon_i \quad \rightarrow \quad \varepsilon_i \sim i.i.d.\exp(1) \\
    \nu_i &= \phi_i \cdot \eta_i \quad \rightarrow \quad \eta_i \sim i.i.d.\exp(1) \\
    s_i &= \varphi_i \cdot \sigma_i \quad \rightarrow \quad \sigma_i \sim i.i.d.\exp(1)
\end{align*}
\]

(2.1.1) (2.1.2) (2.1.3)

Where, the conditional mean is as follows:

\[
\ln(\mu_i) = \gamma + A_1 \ln(\mu_{i-1}) + \ldots + A_q \ln(\mu_{i-q}) + B_0 \ln(\tau_i) + B_1 \ln(\tau_{i+1}) + \ldots + B_p \ln(\tau_{i+p})
\]

(2.1.4)

\(\mu_i' = (\psi_i, \phi_i, \varphi_i)\), \(\tau_i' = (d_i, \nu_i, s_i)\), \(\gamma\) is the vector of coefficients and \(A_1, ..., A_q\) and \(B_0, ..., B_p\) are coefficients matrices of each stochastic processes.
So, the general formulation of the complete model can be written as:

**Observation equation:**

\[
\begin{bmatrix}
  x_i \\
  v_i \\
  s_i
\end{bmatrix} =
\begin{bmatrix}
  \psi_i & 0 & 0 \\
  0 & \phi_i & 0 \\
  0 & 0 & \varphi_i
\end{bmatrix}
\begin{bmatrix}
  \epsilon_i \\
  \eta_i \\
  \sigma_i
\end{bmatrix}
\] (2.1.5)

Where, \( \epsilon_i, \eta_i, \varphi_i \sim \exp(1) \).

**State equation:**

\[
\begin{align*}
\ln \frac{\psi_i}{\phi_i} &= a_0 + \sum_{l=1}^{q} b_{1l}^{(l)} b_{2l}^{(l)} b_{3l}^{(l)} \ln \frac{\psi_{i-l}}{\phi_{i-l}} \\
\ln \frac{\phi_i}{\varphi_i} &= b_4 + \sum_{m=1}^{p} c_{4m}^{(m)} c_{5m}^{(m)} c_{6m}^{(m)} \ln \frac{\phi_{i-m}}{\varphi_{i-m}} \\
\ln \frac{x_i}{v_i} &= c_4 + \sum_{m=1}^{p} d_{4m}^{(m)} d_{5m}^{(m)} d_{6m}^{(m)} \ln \frac{x_{i-m}}{v_{i-m}}
\end{align*}
\] (2.1.6)

2.2 Ordered Probit Model:

In 1992 Hausman, Lo and MacKinlay proposed an alternative statistical model to capture market price changes, based on the techniques usually employed in empirical studies of naturally ordered enumerable dependent variables.

Heuristically, the ordered probit model corresponds to a generalization of the linear regression model, in which the dependent variable is discrete. It is the only specification that captures, in a simple way, both the impact of the variables considered in the formulation and the irregular time interval between trades.

**Basic specification:**

Let a certain transaction price sequence as being: \( P(t_0), P(t_1), ..., P(t_n) \) regarding time \( t_0, t_1, ..., t_n \), and consider \( Y_1, Y_2, ..., Y_n \) the observed price changes \( Y_k = P(t_k) - P(t_{k-1}) \). Due to the discreteness of price, \( Y_k \) could be represented as a multiple of the tick\(^1\). Taking \( Y_k^* \) as being a certain non-observed continuous stochastic variable:

\[
Y_k^* = X_k^* \cdot \beta + \epsilon_k \] (2.2.1)

\[
E[\epsilon_k | X_k] = 0 \] (2.2.2)

\[
\epsilon_k \sim INID N(0, \sigma_k^2) \] (2.2.3)

\(^1\)Tick: minimum amount in which the assets are quoted.
Where, the qx1 vector $X_k = [X_{1k} \ldots X_{qk}]'$ corresponds to the variable set being considered ($Y_k^*$’s conditional mean formulation) and “INID” indicates that the residual sequence ($\epsilon_k$’s) is independently but non-identically distributed. This is one of the most important differences between ordered probit and the standard econometric formulations.

The main characteristic of the ordered probit models is the assumption that the observed price changes ($Y_k$) are related to the variable $Y_k^*$, through the following probabilistic model:

$$
Y_k = \begin{cases} 
  s_1 & \rightarrow \ Y_k^* \in A_1 \\
  s_2 & \rightarrow \ Y_k^* \in A_2 \\
  \vdots & \\
  s_m & \rightarrow \ Y_k^* \in A_m 
\end{cases}
$$

(2.2.4)

Where, $A_i$’s are state space partitions $S^*$ of $Y_k^*$, or, $S^* = \bigcup_{j=1}^{m} A_j$ and $A_i \cap A_j = \emptyset$ to $i \neq j$ and $s_j$’s are discrete values that comprehend the state space $S$ of $Y_k$. In order to simplify the subsequent procedures, the partitions of the space state $S^*$ could be taken as fixed intervals.

$$
A_1 \equiv (-\infty, \alpha_1] 
$$

(2.2.5)

$$
A_2 \equiv (\alpha_1, \alpha_2] 
$$

(2.2.6)

$$
\vdots 
$$

$$
A_i \equiv (\alpha_{i-1}, \alpha_i] 
$$

(2.2.7)

$$
\vdots 
$$

$$
A_m \equiv (\alpha_{m-1}, \infty) 
$$

(2.2.8)

Despite the fact that asset price changes could be any integer number, it’s assumed that “m” (2.2.4) is finite, limiting the parameters set that will be estimated. Such procedure does not introduce problems to the modeling, since that states could represent multiple values of the observed price changes. For example, let $s_k$ as being the price change of -5 ticks or less, and $s_i$ as the price change of 6 ticks or more; in that way, the model does not distinguish between price changes of 6 or more and -5 or less.

Regarding the number of states, the choice will depend on the type of analysis and it won’t be connected to model’s accuracy, when considering large sample. In the case of small samples, the addition of extra states could represent a problem, especially for the estimation process.

In reality, the data will impose the limits to the number of states to be considered, once there won’t be any observation that lies into the “extreme states”, making its estimation impossible.
Conditional distribution of price changes:

As mentioned before, the residuals $\varepsilon_k$’s (2.2.3) are not identically distributed, when conditioned to a certain state ($X_k$’s). The main reason for that assumption is the irregular and random form of time distance between successive trades. If, for example, the price changes ($Y_k^*$’s) could be described by the Arithmetic Brownian Motion (as proposed by Marsh e Rosenfeld - 1986) with variance proportional to $\Delta t_k = t_k - t_{k-1}$, so $\sigma^2_k$ would be a linear function of $\Delta t_k$, which varies from transaction to transaction.

In order to deal with heteroskedasticity, $\sigma^2_k$ will be taken as a linear function of a predetermined variables vector $W_k = [W_{1k} \ldots W_{Lk}]'$, such that:

$$
E[\varepsilon_k | X_k, W_k] = 0, \quad \varepsilon_k \text{INID } N(0, \sigma^2_k)
$$

(2.2.9)

$$
\sigma^2_k = \gamma_0^2 + \gamma_1^2 \cdot W_{1k} + \ldots + \gamma_L^2 \cdot W_{Lk}
$$

(2.2.10)

Where, (2.2.9) and (2.2.10) substitute the hypothesis embedded in equations (2.2.1), (2.2.2) and (2.2.3), and the conditional volatility coefficients ($\gamma$) are squared, what guarantees the non-negativity. In that generic formulation, the propose of Marsh e Rosenfeld (1986) could be easily considered, being necessary the following substitutions:

$$
X_k' \cdot \beta = \mu \cdot \Delta t_k
$$

(2.2.11)

$$
\sigma^2_k = \gamma^2 \cdot \Delta t_k
$$

(2.2.12)

In that case, $W_k$ has just one variable ($\Delta t_k$). The fact of the same variable has been considered in $X_k$ e $W_k$ does not causes perfect multicolinearity, because the first affects the conditional mean of $Y_k^*$, and the other influences the conditional variance.

The structure of dependency imposed in observed price changes process ($Y_k$) is clearly connected to $Y_k^*$ and the definition of $A_j$’s.

$$
P(Y_k = s_j | Y_{k-1} = s_j) = P(Y_k^* \in A_j | Y_{k-1}^* \in A_j)
$$

(2.2.13)

As a consequence, if $X_k$ and $W_k$ are independent through time, the process $Y_k$ (observed) will be too. That assumption is less restrictive, and does not make any of the subsequent statistical inferences invalid. The only assumption that must be preserved is related to the conditional independency of residuals ($\varepsilon_k$’s). In that way, the dynamic (serial dependency) observed in the variable is captured by $X_k$ and $W_k$. Consequently, the independence of $\varepsilon_k$’s does not necessarily imply that $Y_k^*$’s are independently distributed, once none restriction about serial dependency of $X_k$’s e $W_k$’s is made.

The observed price change ($Y_k$) distribution, conditioned to $X_k$ e $W_k$, could be determined considering the partitions boundaries and the probability distribution function of $\varepsilon_k$. In case of normally distributed residuals (Gaussian distribution), the conditional distribution will be:

$$
P(Y_k = s_j | X_k, W_k) = P(X_k' \cdot \beta + \varepsilon_k \in A_j | X_k, W_k)
$$

(2.2.14)
Where,

\( \sigma_k(W_k) \) – conditional standard-deviation as function of \( W_k \)’s;

\( \Phi(.) \) – accumulated probability distribution function (standard Normal).

It could be noticed that the probability associated with a specific price change is determined from the position of the conditional mean regarding the state space partitions boundaries. Besides that, given a certain value for the conditional mean \( X_k^\beta \), any change in the position of the partitions, will affect the probability of each state.

As mentioned before, the ordered probit model can be used with different probability distribution functions – residual term.

In that way, given the partition’s boundaries, a big value for the conditional mean, would indicate a high probability of an “extreme state” being observed. But, the denomination of the state can be “occult” (choice of the number of partitions).

Another advantage of the model presented here is related to the use of economic variables in vectors \( X_k \) and \( W_k \), making possible the determination of the type and magnitude of their influence.

As the estimation process of partition’s boundaries \( \alpha, \beta \) coefficients and conditional variance \( \sigma_k^2 \) is based on the sample’s information (data-driven), then ordered probit model captures empirical relation between the non-observed continuous state space \( S^* \) and the observed discrete state space \( S \), as function of economic variables \( X_k \) e \( W_k \).

**Estimation process (maximum likelihood method):**

Let \( I_k(i) \) as being an indicative variable, which assumes an unitary value, when the realization of k-th observation of \( Y_k \) corresponds to the i-th state \( s_i \), and zero otherwise. Thus, the conditional log-likelihood function \( L \) of the vector of price changes \( Y = [Y_1 \ Y_2 \ ... \ Y_n]' \), conditioned on the explicative variables vector \( X = [X_1 \ X_2 \ ... \ X_n]' \) e \( W = [W_1 \ W_2 \ ... \ W_n]' \) will be:
\begin{align*}
L(\mathbf{y}|X, W) &= \sum_{k=1}^{n} \{A_k + B_k + C_k\} & (2.2.17)
\end{align*}

Where,
\begin{align*}
A_k &= I_k (1) \log \Phi \left( \frac{\alpha_i - X_i/\beta}{\sigma_k(W_k)} \right) & (2.2.18)
B_k &= \sum_{i=2}^{m-1} I_k(i) \log \left[ \Phi \left( \frac{\alpha_i - X_i/\beta}{\sigma_k(W_k)} \right) - \Phi \left( \frac{\alpha_{i-1} - X_i/\beta}{\sigma_k(W_k)} \right) \right] & (2.2.19)
C_k &= I_k(m) \log \left[ 1 - \Phi \left( \frac{\alpha_{m-1} - X_i/\beta}{\sigma_k(W_k)} \right) \right] & (2.2.20)
\end{align*}

Despite of the fact that \( \sigma_k^2 \) has been defined as a linear function of \( W_k \), there are some restrictions that must be imposed to the parameters, making possible the identification of them. For example, the log-likelihood function value would remain the same, if a certain constant \( K \) multiplied the values of \( \alpha \)'s, \( \beta \)'s and \( \sigma_k^2 \). A typical procedure is to define \( \gamma_0 = 1 \).

There are three basic steps to be followed before initialize the estimation process:

- The determination of the number of states \( m \);
- The definition of the regressors being considered;
- The specification of the conditional variance \( \sigma_k^2 \).

As commented already, the definition of the number of states should be based on the observed price changes empirical distribution. Such procedure will avoid the adoption of a state with no observations.

Regarding the regressors definition, it will depend on the type of analysis and objectives. If they are related to forecasting, in general, the use of lagged price changes and market indices contribute to good results.

**Price model (Ordered Probit Model):**

Let \( z_i \) as the price changes of a specific asset expressed in tick units. Thus, based on equations (2.2.1) and (2.2.10), the proposed formulation is defined as follows:

\begin{align*}
z_i &\sim N(\mu_i, \sigma_i^2) & (2.2.21)
\mu_i &= \sum_{k=0}^{3} (a_k \cdot x_{i-k} + b_k \cdot u_{i-k} + c_k \cdot s_{i-k}) + \sum_{n=1}^{3} (d_n \cdot z_{i-n}) & (2.2.22)
\sigma_i^2 &= \gamma_0 \cdot x_i + \gamma_1 \cdot s_{i-1} & (2.2.23)
\end{align*}
Where, \((a_0, \ldots, a_3, b_0, \ldots, b_3, c_0, \ldots, c_3, d_1, \ldots, d_3, \gamma_0, \gamma_1)\) are the parameters to be estimated, \(x_i\) is the duration, \(v_i\) is the volume and \(s_i\) the bid-ask spread of the \(i\)-th event.

### 3 Empirical Analyses

#### 3.1 Data Base:

The database used in the empirical analysis presented in this article was built by Joel Hasbrouck e NYSE – Trades, Orders Reports and Quotes (TORQ). The data reflect the trades of IBM stocks, occurred between November 1\textsuperscript{st}, 1990 and November 16\textsuperscript{th}, 1990.

The database comprehends all the relevant information embedded in financial transactions – buys or sells (i.e., bid price, ask price, transaction price, time and volume) registered during regular financial market time – 9:30 AM - 4:00 PM (after-market is not considered).

In order to get the basis for the development of the study, some changes were implemented in the original data. Such procedure was necessary, due to the nature of the existent information.

Each one of the registers in the original database refers to a transaction that has effectively occurred. Since that study will focus on the modeling of tick-by-tick (price change) data and not in an event basis analysis, it was necessary to group the relevant information.

- **Duration:**
  - If the price of transaction “\(i\)” is equal to the price of transaction “\(i-1\)”, so duration “\(i\)” is equal to the sum of durations “\(i\)” and “\(i-1\)”;
  - If a certain transaction (with price change) presents duration equal to zero, so that register is discarded.

- **Volume:**
  - If the price of transaction “\(i\)” is equal to the price of transaction “\(i-1\)”, so volume “\(i\)” is equal to the mean of the volumes of transactions “\(i\)” and “\(i-1\)”.

- **Spread:**
  - Spread “\(i\)” is equal to the difference between bid price “\(i\)” and ask price “\(i\)”;
  - If the price of transaction “\(i\)” is equal to the price of transaction “\(i-1\)”, so spread “\(i\)” is equal to the mean of the spreads of transactions “\(i\)” and “\(i-1\)” weighted by the volumes of such transactions (bid-ask spread may change according to the volume being traded through an specific market-maker).

relevant changes and considerations:

- The tick-by-tick series has the unity value of the tick as reference (US$ 0.125);
The transaction occurred during the first twenty minutes of trading day were not considered for estimation purposes (9:30 AM - 9:50 AM) – opening postponing problems and “first trades” effects;

For each day, the conditional mean of each one of the variables of the system (deseasonalized series) will be taken as the mean of the respective values observed between 9:50 AM e 10:00 AM (if there are no observations, the conditional mean is taken as one).

3.2 Empirical tests:

The empirical tests could be divided into different stages with distinct objectives.

1) Five consecutives trading days are selected from the database (01/11/1990 – 08/11/1990) and EMACM (2,2) is estimated just considering the variables existent in the price model (duration, bid-ask spread and volume). Figures 1 – 5 present the results of the in-sample analysis.

- ACF

  o Duration

  ![Figure 1 – ACF of duration (residuals x observations)](image)

  - Volume

  ![Figure 2 – ACF of volume (residuals x observations)](image)
○ Spread

![Figure 3 – ACF of spread (residuals x observations)](image)

- Ljung-Box:

<table>
<thead>
<tr>
<th></th>
<th>Accept H0 (95%)</th>
<th>P Value</th>
<th>Ljung-Box</th>
<th>Critical Value</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Observations</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Duration</td>
<td>Reject</td>
<td>0.00%</td>
<td>68.52</td>
<td>25.00</td>
</tr>
<tr>
<td>Volume</td>
<td>Reject</td>
<td>0.00%</td>
<td>88.34</td>
<td>25.00</td>
</tr>
<tr>
<td>Spread</td>
<td>Reject</td>
<td>0.00%</td>
<td>94.88</td>
<td>25.00</td>
</tr>
<tr>
<td><strong>Residuals</strong></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(08/11/1990)</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Duration</td>
<td>Accept</td>
<td>28.89%</td>
<td>17.34</td>
<td>25.00</td>
</tr>
<tr>
<td>Volume</td>
<td>Accept</td>
<td>17.08%</td>
<td>12.10</td>
<td>25.00</td>
</tr>
<tr>
<td>Spread</td>
<td>Accept</td>
<td>11.59%</td>
<td>21.55</td>
<td>25.00</td>
</tr>
</tbody>
</table>

Table 1 – Linear dependency analysis (Ljung-Box test)

2) Ordered Probit Model as described in (2.2.21), (2.2.22) and (2.2.23) is estimated. Through the use of EMACM forecasting function, the one-step-ahead forecast is generated and its results are used as substitutes to the contemporaneous variables value in the Ordered Probit Model formula (price model’s forecasting function). The partitions selected by the price model’s forecasting function are then checked against the real data and the one selected by NAIVE rule\(^2\). In this part, the time period from 08/11/1990 until 16/11/1990 is tested based on a five days period. The main objective is to present the out-of-sample price model forecasting results (Appendix I brings the main results observed).

- **Unconstraint model**: the econometric model estimates the partitions boundaries and coefficient matrices. Figure 4 present the results found. Here, the number of right choices (one-step-ahead price movements) of the proposed model is compared against NAIVE, as described before.

---

\(^2\) NAIVE rule: if a certain partition X is selected in a given event “i”, then, for the subsequent event, the partition will remain the same.
• **Direction:** the main objective of that procedure is to test the capability to forecast just the direction of the prices movements and not the magnitude of them. In that experiment the partition is fixed in zero and the only the equation’s parameters have to be estimated.

As can be notice the proposed method captures quite satisfactory the intra-day pattern and the dynamic embedded in price changes. Figure 6 summarizes the results.
The results point to the existence of a intra-day pattern that is captured by the proposed model. Despite of the fact that trades, when analyzed together, do not present significant asymmetry (see results in Appendix I). When the chronological sequence of events is taken and modeled properly, intra-day behavior could conduct to some predictability when considering price movements (conditional distribution).

4 Conclusion and Final Comments

In this article, the challenge of stock price forecasting is faced through the use of an integrated approach in which the modeling of high frequency financial data (duration, volume and bid-ask spread) uses a contemporaneous ordered probit model in which price changes (measured in numbers of ticks) are the interest variable. Here, the formulation introduced by Raposo and Veiga (2004) – EMACM – was used in order to capture the dynamic that high frequency variables present, and its forecasting function is taken as proxy to the contemporaneous information necessary to the proposed price model.

Regarding high frequency data model, excellent results were obtained when considering the linear dependence observed in the original series. If compared with the results presented by the authors in the original article (one month sample), these could be considered better in terms of fitting. Another interesting point is that non-linear dependencies (excess of dispersion) weren’t so significant.

When the method (high frequency data and ordered probit models) is tested against NAIVE rule, the results show that the use of high frequency variables in order to forecast intra-day price changes is really effective. Both, the intra-day pattern and variables dynamics are satisfactory captured.

In general lines, the main objective of the paper was achieved and the integrated approach proposed here shows itself robust when dealing with one of most exciting questions.
5 Bibliographies


### Appendix I

<table>
<thead>
<tr>
<th>Date</th>
<th>Model type</th>
<th>Model specification</th>
<th>Partition</th>
<th>Observations</th>
<th>Model (real data)</th>
<th>NAIVE</th>
<th>Observations</th>
<th>Model (forecasting)</th>
<th>NAIVE</th>
</tr>
</thead>
<tbody>
<tr>
<td>03/11/1990</td>
<td>Unconstraint</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>148</td>
<td>59</td>
</tr>
<tr>
<td></td>
<td>Direction</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>162</td>
<td>59</td>
</tr>
<tr>
<td>09/11/1990</td>
<td>Unconstraint</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>209</td>
<td>48</td>
</tr>
<tr>
<td></td>
<td>Direction</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>209</td>
<td>50</td>
</tr>
<tr>
<td>12/11/1990</td>
<td>Unconstraint</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>345</td>
<td>73</td>
</tr>
<tr>
<td></td>
<td>Direction</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>337</td>
<td>75</td>
</tr>
<tr>
<td>13/11/1990</td>
<td>Unconstraint</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>195</td>
<td>47</td>
</tr>
<tr>
<td></td>
<td>Direction</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>195</td>
<td>47</td>
</tr>
<tr>
<td>14/11/1990</td>
<td>Unconstraint</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>179</td>
<td>48</td>
</tr>
<tr>
<td></td>
<td>Direction</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>179</td>
<td>50</td>
</tr>
<tr>
<td>15/11/1990</td>
<td>Unconstraint</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>148</td>
<td>32</td>
</tr>
<tr>
<td></td>
<td>Direction</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>162</td>
<td>32</td>
</tr>
<tr>
<td>16/11/1990</td>
<td>Unconstraint</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>135</td>
<td>50</td>
</tr>
<tr>
<td></td>
<td>Direction</td>
<td>EMACM(2,2)</td>
<td>-1 0.00 0.00</td>
<td>0</td>
<td>10</td>
<td>0</td>
<td>10</td>
<td>172</td>
<td>53</td>
</tr>
</tbody>
</table>