

# Picturing mobility: Transition probability color plots

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2011 London Stata Users Group meeting  
September 15–16 2011, Cass Business School, London

# Income mobility

- ▶ Analysis of change over time in individual income and of the distribution thereof  
(see, e.g., *Changing Fortunes* by Jenkins (2011))
- ▶ Classic summary: the *transition matrix*
  - ▶ incomes at two points in time
  - ▶ partition population (or sample) into income groups –most often by quantile groups– at both periods
  - ▶ report probabilities  $p_{ij}$  of transition to group  $j$  conditional on starting in group  $i$  ( $\sum_j p_{ij} = 1$ )

# Transition matrices

## Quintile groups:

Origin	Destination				
	1	2	3	4	5
1	0.36	0.24	0.16	0.13	0.11
2	0.18	0.24	0.25	0.22	0.11
3	0.13	0.18	0.26	0.26	0.17
4	0.16	0.16	0.18	0.25	0.24
5	0.08	0.08	0.13	0.24	0.46

Misses details and/or  
difficult to read and  
compare

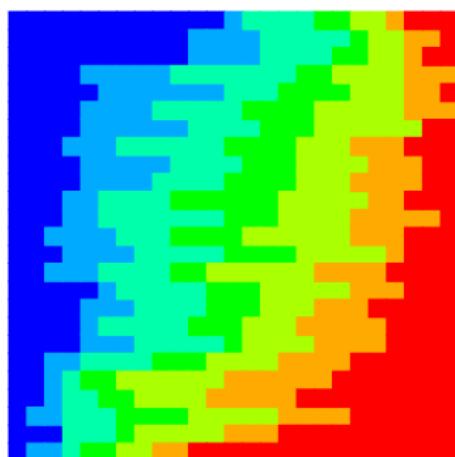
## Decile groups:

Origin	Destination									
	1	2	3	4	5	6	7	8	9	10
1	0.25	0.19	0.07	0.10	0.08	0.07	0.06	0.05	0.08	0.04
2	0.13	0.15	0.16	0.15	0.08	0.10	0.08	0.07	0.06	0.03
3	0.07	0.10	0.15	0.10	0.14	0.12	0.15	0.10	0.04	0.03
4	0.08	0.10	0.11	0.12	0.11	0.13	0.09	0.10	0.10	0.06
5	0.05	0.07	0.09	0.10	0.12	0.14	0.13	0.13	0.11	0.05
6	0.07	0.07	0.06	0.11	0.12	0.12	0.16	0.10	0.12	0.07
7	0.08	0.10	0.06	0.09	0.12	0.09	0.13	0.10	0.12	0.10
8	0.10	0.04	0.05	0.11	0.06	0.10	0.12	0.16	0.12	0.14
9	0.05	0.04	0.06	0.04	0.05	0.10	0.11	0.20	0.16	0.20
10	0.04	0.04	0.03	0.03	0.07	0.05	0.07	0.10	0.15	0.42

## The transition matrix pictured...

A visual representation of the transition matrix: the *Transition probability color plot*

Transition probability color plot



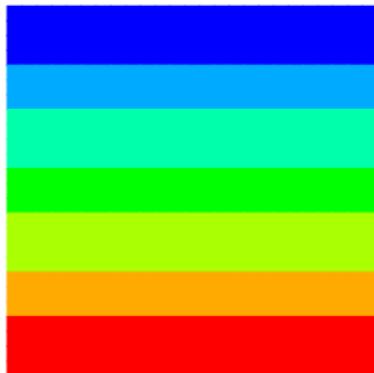
Each block is a (small) fraction of population/sample, arranged so that:

- ▶ Low income groups at top to high income groups at bottom (**origin**)
- ▶ Low income groups in blue to high income groups in red (**destination**)

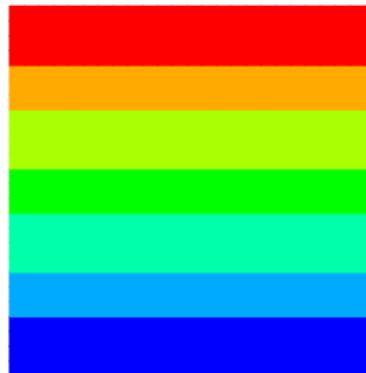
# Benchmarks

Benchmark pictures: status quo (immobility), reversal (total mobility), independence

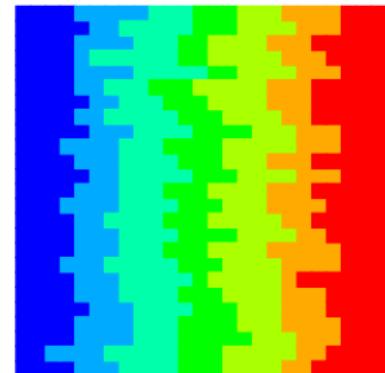
STATUS QUO



COMPLETE REVERSAL



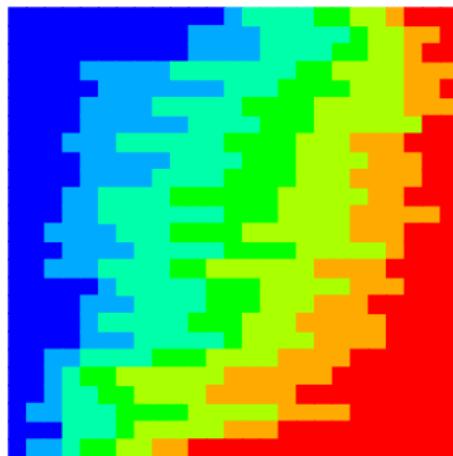
INDEPENDENCE



## Reverse estimates

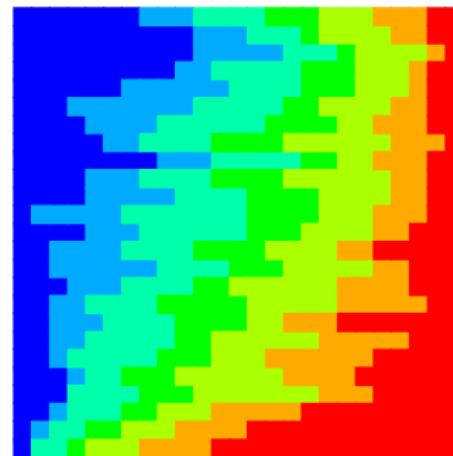
Alternative representation: Arrange from top to bottom according to **destination** income group and color according to **origin** income group:

Transition probability color plot



Transition probability color plot

(reversed plot)



## Stata command: `transcolorplot`

The command `transcolorplot` will be available from the SSC archive

### Syntax

```
transcolorplot varname1 varname2 [if] [in] [weight]  
[, nquantiles(#) nbins(#) ncolors(#) reverse ... ]
```

where '...' are various options for (i) saving plot coordinates, (ii) for color rendition and (iii) miscellaneous additional graphical options

## Implementation: Sitting on a giant's shoulders

`transcolorplot` sits on a giant's shoulders: the user-written commands `spmap` and `spgrid` by Maurizio Pisati (both available on SSC, see Pisati (Stata Journal, 2004)).

`transcolorplot` does relatively little:

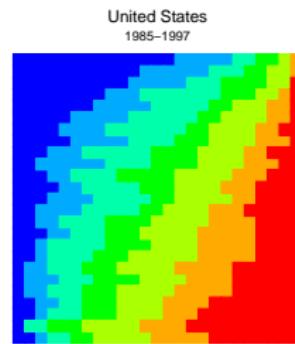
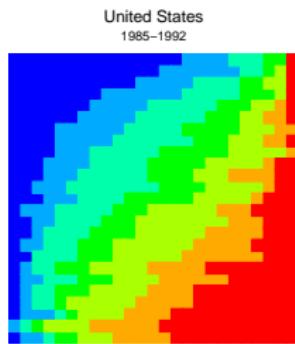
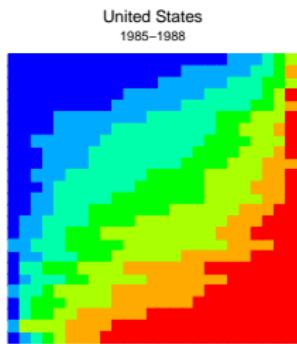
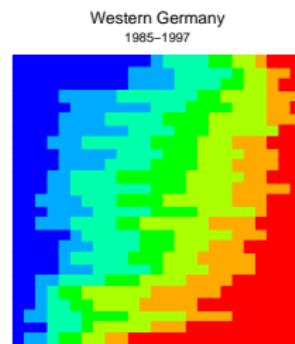
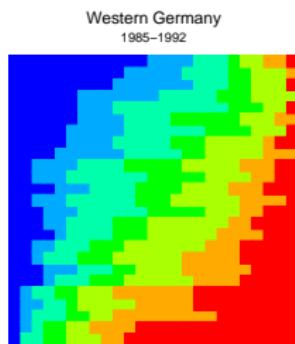
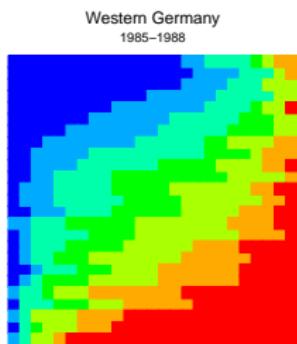
1. arranges data into  $n_{quantiles} \times nbins$  cells and evaluates cell 'value' (according to origin and destination incomes)
2. calls `spgrid` to generate a two-dimensional grid (the 'chessboard')
3. calls `spmap` to colorize the chessboard according to cell values computed at step 1 and draw the picture

All drawing options are passed to `spmap`: control for color palette, labels and titles, added text, overlaid labels and points, etc.

## Example 1: Individual income mobility in USA and Germany

- ▶ Panel Study on Income Dynamics (USA) and German Socio-economic Panel survey (Western Germany)
- ▶ Data extracted from the Cross-National Equivalent data files –as used in Van Kerm (Economica, 2004)
- ▶ Panel data on household income in 1985, 1988, 1992 and 1997
- ▶ Approx. 6,000 observations in both countries (for balanced sample)
- ▶ After tax, total annual disposable household income adjusted for household size

# Example 1: Individual mobility in USA and Germany

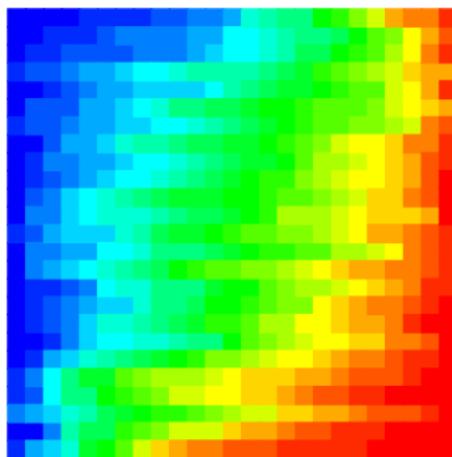


## Some possible variations...

More detailed color palette

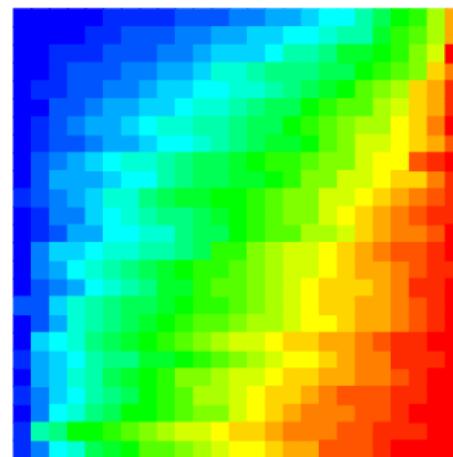
Western Germany

1985–1997



United States

1985–1997



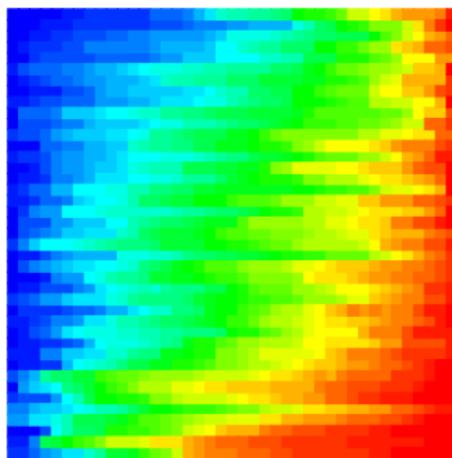
More informative?

## Some possible variations...

Finer grid

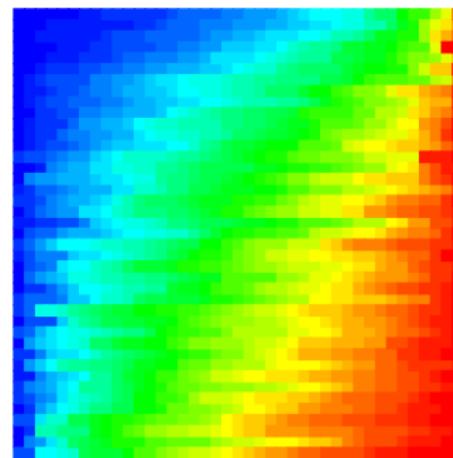
Western Germany

1985–1997



United States

1985–1997



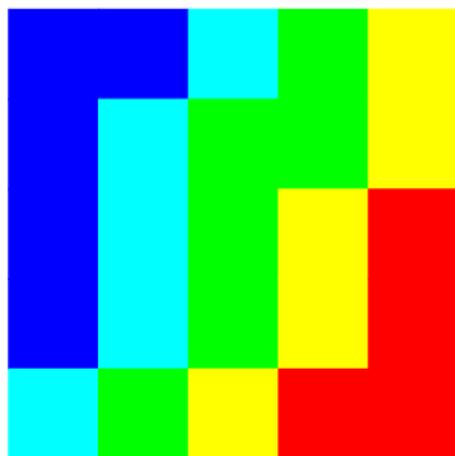
More informative?

# Some possible variations...

Less details!

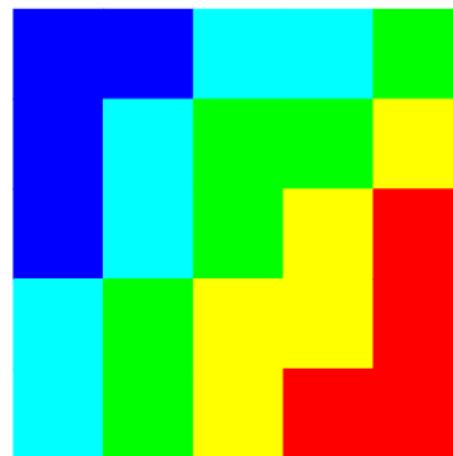
Western Germany

1985–1997



United States

1985–1997



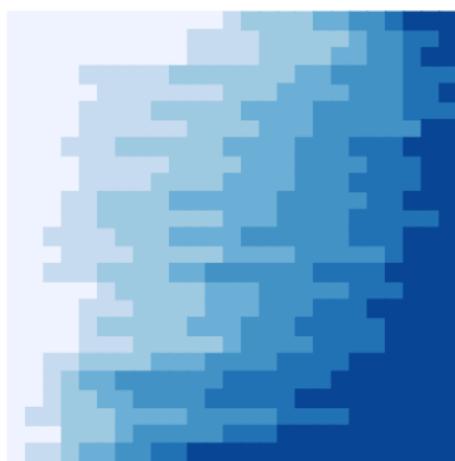
Notice rounding issues!

## Some possible variations...

### Alternative palettes

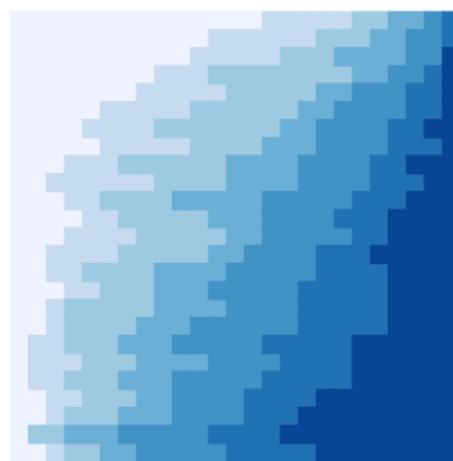
Western Germany

1985–1997



United States

1985–1997

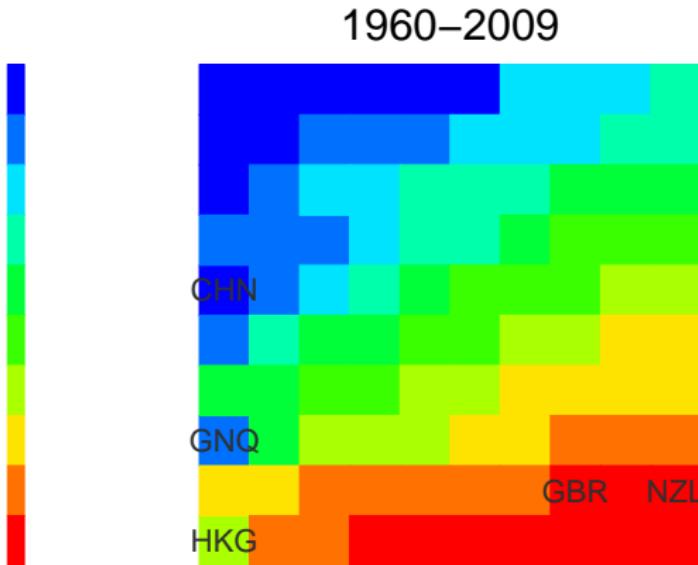


Color palettes provided by `spmap`  
(default is ‘rainbow’, here ‘blues’)

## Example 2: International mobility in GDP per capita over 50 years

- ▶ Data from the Penn World Tables
- ▶ GDP per capita adjusted to common prices with purchasing power parities
- ▶ 100 countries with complete data from 1960–2009 (as used in O'Neill & Van Kerm (Manchester School, 2008))

# Mobility in GDP per capita over 50 years



- ▶  $10 \times 10$  grid: each cell is just one country
- ▶ ‘reverse’ plot: countries ordered from top to bottom by destination (2009) GDP with color based on origin (1960) GDP

# Mobility in GDP per capita over 50 years

How did we get there? Some animated plots...

(click on 'play' button to run!)

# Mobility in GDP per capita over 50 years

Mobility in 1970–1989 vs. 1990–2009

(click on ‘play’ button to run!)

## Acknowledgements

*This work is part of the PersiPov project supported by the Luxembourg ‘Fonds National de la Recherche’ (contract C10/LM/783502).*